

IES / GATE

Electrical Engineering

VOLUME-III

**Basic Electronics Engineering
Control System**

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ELECTRONIC DEVICES & CIRCUITS

1. Integrated Electronics
by Millman Halkias
2. Micro Electronics
by Sedra & Smith.
3. Electronic's devices & circuits.
By Neamen.

Classification of Temperature:

- (1) Absolute temp $0K = -273C$
- (2) Room Temp $300K = 27C$ [for semiconductor devices by default this temp is considered]
- (3) Ambient Temp $[T_A] 290K = 17C$
(Surrounding Temp). [for communication system Ambient temp] took as default temp.]

$$\text{Temp in } ^\circ C = \text{Temp in Kelvin} - 273$$

$$^{\circ}K = K$$

Thermal voltage :- (V_T) :-

* "Volt equivalent of temperature"

$$V_T = \frac{KT}{q}$$

 volt.

k (Boltzman Constant):

$$K = 1.381 \times 10^{-23} \text{ J/K.}$$

$$k = 8.62 \times 10^{-5} \text{ eV/K.}$$

T = Temperature, in K
 q = magnitude of charge
 $= 1.6023 \times 10^{-19} \text{ coulomb}$
 $= 1.381 \times 10^{-23} \text{ J/K.}$

$$V_T = \frac{T}{11600} \text{ volt.}$$

$$V_T \propto T$$

If $T = 0K$ $V_T = 0$

If $T = 300K$ $V_T = \frac{300}{11600} = 0.02568 \text{ volt}$
 $= 26 \text{ mV.}$

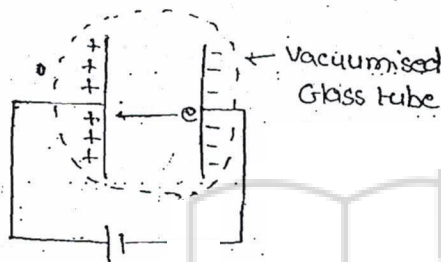
The standard room temperature corresponds to a voltage of 26mV.

∴ For a large variation in temperature we get a minute variation in thermal voltage.

Electron volt (eV):-

* It is the practical unit of energy in electronics.

* 1 eV is defined as the energy gain by the electron in moving through a potential difference of 1 volt.



$\epsilon_r(\text{air}) = 1.01 \approx 1$

$\epsilon_r(\text{Vacuum}) = 1$

$$1 \text{ eV} = |q| \times P.D.$$

$$= 1.6 \times 10^{-19} \times 1 \text{ volt}$$

$$= 1.6 \times 10^{-19} \text{ Coulomb-Volt or Joule.}$$

$1 \text{ eV} = 1.6 \times 10^{-19} \text{ Joule.}$

* Electron volt indicates the kinetic energy gained by the electron or potential energy lost by the electron.

$$K.E. = \frac{1}{2} m v^2$$

\downarrow mass of e^- ($9.1 \times 10^{-31} \text{ k.g.}$)

$$P.E. = q \cdot V$$

$$K.E. \text{ gained} = P.E. \text{ loss}$$

$$\frac{1}{2} m v^2 = qV$$

Velocity of e^- $v = \sqrt{\frac{2qV}{m}}$ meter/sec

Electric Field Intensity (E or \vec{E}):-

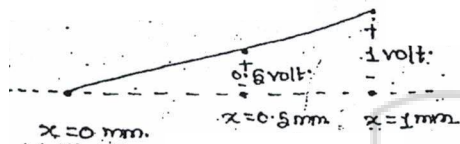
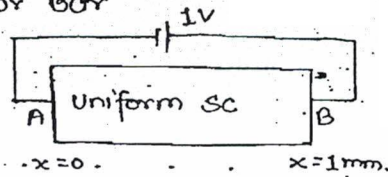
Normally called as field intensity, field gradient or field.

By Definition

$\vec{E} = -\frac{dV}{dx} \text{ volt/meter}$

$$|E| = \frac{|\text{Voltage existing}|}{\text{spacing or distance}}$$

Ex. Considering a uniform semiconductor bar



Magnitude of field intensity at end B.

$$|E|_B = \frac{|V_B|}{x_B} = \frac{1 \text{ volt}}{1 \times 10^{-3} \text{ m}} = 10^3 \text{ V/m.}$$

Magnitude of field at centre of bar.

$$|E|_C = \frac{|V_C|}{x_C} = \frac{0.5}{0.5 \times 10^{-3}} = 10^3 \text{ V/m.}$$

$$|E|_A = \frac{|V_A|}{x_A} = \frac{0}{0} = \text{undefined.}$$

Mobility of Charge Carrier (μ):-

Mobility denotes the current carrying capacity or how fast the charge carrier is moving from one place to another place.

Mobility is defined as drift velocity to field intensity

$$\mu = \frac{V_d}{E} \quad \text{m}^2/\text{V}\cdot\text{sec} \text{ or } \text{cm}^2/\text{V}\cdot\text{sec}$$

$$\mu = \frac{\text{Drift Velocity}}{\text{Field Intensity}}$$

e^- mobility (μ_n or μ_e)

hole mobility (μ_p or μ_h)

μ	Ge	Si
μ_e	3800 $\text{cm}^2/\text{V}\cdot\text{sec}$	1300 $\text{cm}^2/\text{V}\cdot\text{sec}$
μ_p	1800 $\text{cm}^2/\text{V}\cdot\text{sec}$	500 $\text{cm}^2/\text{V}\cdot\text{sec}$

$$\frac{\mu_n}{\mu_p} = 2.1 \quad (\text{for Ge})$$

$$\frac{\mu_n}{\mu_p} = 2.6 \quad (\text{for Si})$$

Electron mobility is always greater than hole mobility.

Electron can travel faster & also contribute more current than hole.

Ge $\left\{ \begin{array}{l} \text{Higher Conductivity} \\ \text{(Due to larger mobilities)} \\ \text{Relatively more suitable for high} \\ \text{frequency application [due to large} \\ \text{B.W]} \end{array} \right.$

Si $\left\{ \begin{array}{l} \text{Relatively more suitable for swi} \\ \text{applications (Better thermal} \\ \text{stability).} \\ \text{Best suit for high power applica} \\ \text{(Natural Property).} \end{array} \right.$

Mobility of charge carrier always decreases with the temperature.

As temperature increases atoms of the material will vibrate & due to this thermal vibration or the agitation the mobility of charge carrier

$$\mu \propto T^{-m}$$

where m is constant and is given

as

for Si

for Ge

$$m = 2.5 \text{ for } e^-$$

$$m = 1.66 \text{ for } e^-$$

$$= 2.7 \text{ for hole.}$$

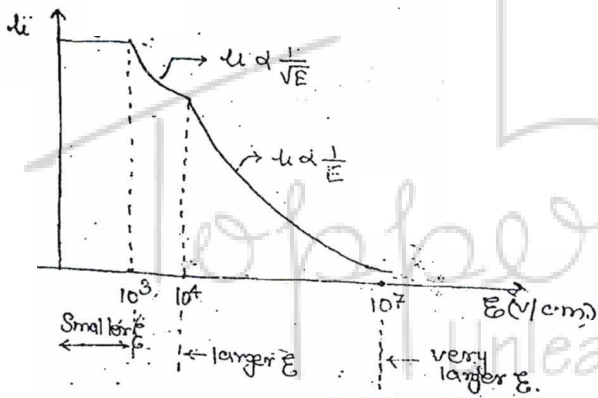
$$= 2.33 \text{ for hole.}$$

mobility decreases with the temperature

as a non linear variation.

μ vs E curve for a S.C. :-

(Experimentally plotted).



Question: when smaller field intensities

are applied to the semiconductor,

(a) mobility of charge carriers remain constant.

(b) drift velocity linearly increases with the field intensity.

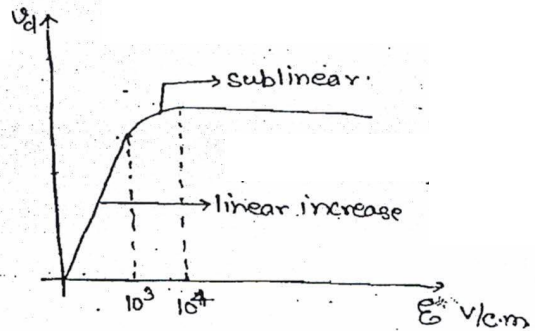
$$V_d = \mu E$$

Question: when larger field intensities are applied to the semiconductor

(a) mobility of the charge carrier decreases.

(b) drift velocity enters into saturation.

V_d vs E curve for S.C. :-



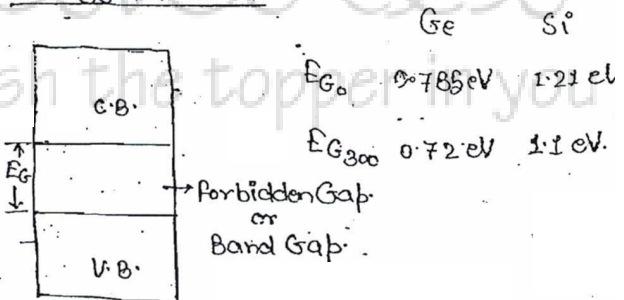
Question: In a semiconductor when field intensity are increasing the drift velocity

(a) linearly increases.

(b) sublinearly increases.

& enters into saturation with larger fields applied.

Energy Gap (E_g) :-



In semiconductor, E_g (or) energy gap decreases with temperature.

$$E_g \propto \frac{1}{\text{Temp}(T)}$$

$$E_g(T) = E_{g0} - \beta_0 T \text{ eV.}$$

β_0 = material constant (eV/°K).

for Si $\beta_0 = 3.6 \times 10^{-4} \text{ eV/}^\circ\text{K}$.

$$E_g(T) = E_{g0} - \beta_0 T$$

for Ge $\beta = 2.33 \times 10^{-4}$

So $E_G(T) = 0.785 - 2.33 \times 10^{-4} T$

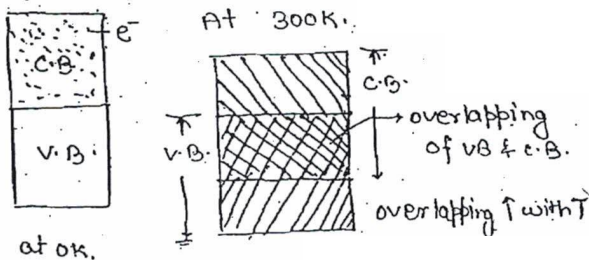
Classification of Elements into conductors, semiconductors, & insulators:-

Conductors or Metals:-

- * Very good conductors of currents.
- * Valence electrons are ≤ 3
- * All metals are unipolar.
- * I, II & III group of periodic table (metallic or non metallic).
- * In metal free e^- concentration is very high.

Concentration of $e^- (n) = 10^{28} / m^3$

- * Metallic bonding is present
- * Energy gap $E_G = 0$ at $0K$.



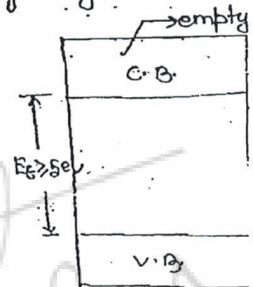
- * In metals free electrons are available even at $0K$.
- In metals free electron concentration is independent of temperature.
- * Because of overlapping a valence band & conduction band metal will exhibit PTC of resistance.

* In metals there is only e^- drift current.

E.g. → Gold, Silver, Tungsten, Platinum, Iridium, Copper, Tin, Iron, Uranium.

Insulators:-

- * Bad conductors of current.
- * Valency electrons are 7 or 8.
- * Ionic bonding
- * NTC (Negative Temperature Coefficient of resistance)
- * Energy gap is very large
- * $E_G \geq 5 eV$.
- * Conductivity is zero for ideal insulators.
- * $\sigma =$ negligible for practical insulators.
- * In insulators E_G (Energy Gap) still decreases with the temperature \uparrow
- * Insulators are subjected to breakdown.



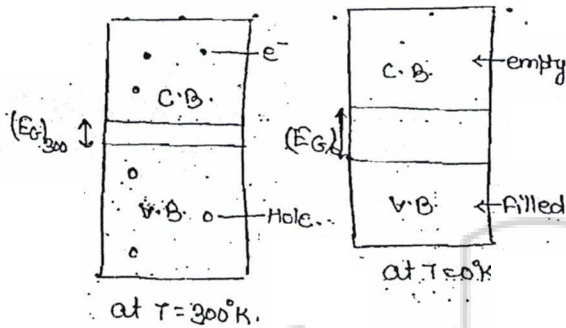
E.g. Diamond, SiO_2 , Air, Mica, ceramic, porcelain, Bakelite, Paper, Rubber, Coal, PVC, Leather, wood, glass, Plastic, fiber.

Semiconductor's (S.C):-

- * Semi-conductors are elements whose conductivity lies between the conductivity of an insulator & conductivity of a conductor.
- * Valence electrons are 4. (IV group below the Si)

2. Covalent Bonding.
3. All semiconductors are insulators at 0°K.
4. Energy gap is small (0.7 eV to 1.5 eV) or ≈ 1 eV.

Energy Band Diagram at 0°K.



5. At 0°K carrier concentrations are zero & therefore conductivity is 0. & semiconductor at 0°K will be working as an insulator.
6. At 300°K because of thermal energy a no. of covalent bond will be broken & equal no. of electron & holes are created & there will be a conductivity in a semiconductor.
7. Semiconductors are Bipolar having two different type of charge carriers - electrons & holes.
8. In a semiconductor there will be a diffusion current.

9. All semiconductors are temperature sensitive.
10. In a sc energy gap decreases with temperature.

$$\text{Eg} \propto \frac{1}{\text{Temperature}}$$

E.g. - Si, Ge...

05/07/2013

Why carbon is not considered as a SC element?

- * Carbon belongs to IV group of the periodic table but it is never considered as a semiconductor element because energy band gap is more than 1.5 eV. It has very unreliable & unpredictable properties.
- Graphite \rightarrow behaves as SC & conducts at different temperature.
- Diamond \rightarrow behaves as

Einstein's Equation:-

- * It was given just as a mark of respect to great physicist Einstein.
- * In a sc

$$\frac{D_n}{\mu_n} = \frac{D_p}{\mu_p} = V_T$$

* It gives the relationship b/w diffusion constant, mobility & thermal voltage

$$\frac{D_n}{\mu_n} = \frac{D_p}{\mu_p} = \frac{1}{\mu} V_T$$

* The unit of mobility to diffusion constant is v^{-1}

* The unit for $\frac{D}{u}$ is volt.

Diffusion Constant of Charge Carriers:-

e⁻ diffusion constant (D_n) = $u_n V_T$
 the hole diffusion constant (D_p) = $u_p V_T$

Unit for $D \rightarrow cm^2/sec$ or m^2/sec

$$D = u V_T$$

* Diffusion constant of charge carrier decreases with the change temp^r.

Diffusion constant for Ge at 300K.

$$D_n \approx 99 cm^2/sec$$

$$D_p \approx 47 cm^2/sec$$

For Si at 300K.

$$D_n = 34 cm^2/sec$$

$$D_p = 13 cm^2/sec$$

$$\frac{D_n}{D_p} = \frac{u_n V_T}{u_p V_T}$$

$$\text{or } \boxed{\frac{D_n}{D_p} = \frac{u_n}{u_p}} \quad \text{or } \boxed{D_n u_p = D_p u_n}$$

For Ge

$$\frac{D_n}{D_p} = 2.1$$

For Si

$$\frac{D_n}{D_p} = 2.6$$

* Diffusion constant is a material const associated with the property called diffusion & it can not be negative.

MASS ACTION LAW:-

$$\boxed{n p = n_i^2}$$

mass action law states that

in a sc. (intrinsic or extrinsic) under

thermal equilibrium the prod of electrons & holes is a constant & it is equal to square of intrinsic concentration

* The law is particularly used extrinsic semiconductors to calculate minority carrier concentration

N-Type Semiconductor

Majority carriers are e⁻s = n;

Minority carriers are holes = p

$$\boxed{p_n = \frac{n_i^2}{n_n}}$$

P-Type Semiconductor:-

Majority carriers are holes = p

Minority carrier are e⁻s = n

$$\boxed{n_p = \frac{n_i^2}{p_p}}$$

~~→~~ In a pure semiconductor

e⁻s & hole concentrations are

respectively by adding impurity atom into the semiconductor

& holes concentration are n

respectively. then following

relation are applicable.

$$\boxed{n_1 p_1 = n_2 p_2 = n_i^2}$$

Intrinsic Concentration (n_i):-

Intrinsic \equiv Pure

$$n = p = n_i$$

$$\boxed{n_i^2 = A_0 T^3 e^{-E_g/KT}}$$

$$n_i = \sqrt{A_0 \cdot T^{3/2} e^{-\frac{E_g}{2KT}}}$$

A_0 = Material constant

* Intrinsic concentration is a function of temperature & energy gap

In a sc, Intrinsic concentration n_i^2 --

(a) T^3 b) $T^{3/2}$

In a sc, Intrinsic concentration n_i is --

(a) T^3 b) $T^{3/2}$

* Intrinsic concentration increases with the temperature as a nonlinear variation

* when compared to Silicon, germanium has larger value of n_i & this is due to smaller value of energy gap.

At room

In Ge, $n_i = 2.5 \times 10^{13} \text{ atom/cm}^3$

Si, $n_i = 1.5 \times 10^{10} \text{ atom/cm}^3$

Resistivity (ρ):

(Specific Resistance)

Unit for $\rho \rightarrow \Omega\text{-cm}$
or $\Omega\text{-m}$

* In metal resistivity increases with temperature.

* In semiconductor resistance decreases with temperature.

Conductivity (σ):

* The Reciprocal of resistivity = $\frac{1}{\rho\text{-m}}$

* q denotes current carrying capacity of device or material

* q denotes current

$$\sigma = \text{Carrier Conc}^n \times q \times \text{mobility}$$

* Conductivity depends on carrier concentration, magnitude of charge

& mobility.

* Conductivity variation may be due to variation in carrier concentration & variation in mobility

$$\sigma = n q \mu_n$$

* In metals conductivity decreases as temperature.

* In metal's free electron concentration is independent of temperature so conductivity does not depend on carrier concentration.

For semiconductors (Bipolar)

$$\sigma = n q \mu_n + p q \mu_p$$

* In intrinsic semiconductor, conductivity increases with the temp.

* In intrinsic semiconductor, as temp increases mobility decreases and this will slightly reduce the conductivity & at the same time because of thermal energy a large no. of covalent bond will be broken & equal no. of e^- & holes are generated

* this will increase the conductivity by a larger value & that's why conductivity increases with temp in intrinsic sc.

* In sc conductivity mainly depends on carrier concentration.

Current Density (J):

It is the current passing per unit area.

$$J = I/A \dots A/m^2 \text{ or } A/cm^2$$

$$J = \sigma E \quad E \rightarrow \text{electric field intensity}$$

In metals

$$\text{Current density (J)} = nq_u E$$

In sc

$$J = nq_u u_n E + Pq_u u_p E$$

$$J = qE (u_n n + P u_p) \quad A/m^2$$

Current:-

* Rate of change of charge is known as current.

$$i = \frac{dq}{dt} \quad \text{Ampere.}$$

Drift Current:-

It is the flow of current through the material or device under the influence of electric field intensity.

Diffusion Current & Diffusion:-

Diffusion is a natural property. Diffusion is defined as the migration of charge carriers from higher concentration to lower concentration.

or from higher density to lower density.

$$\text{Gradient (slope)} = \frac{d}{dx}$$

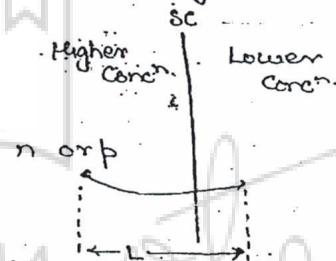
$$\frac{dn}{dx} = e^- \text{ concentration gradient}$$

$$\frac{dP}{dx} = \text{hole concentration gradient}$$

$$\text{Unit } \frac{dn}{dx} = e^- / cm^3 / cm.$$

$$\text{Unit } \frac{dP}{dx} = \text{holes} / cm^3 / cm.$$

* Diffusion is mainly occurred due to concentration gradient.



* Diffusion current flows only in semiconductors.

* In a semiconductor diffusion is due to unequal distribution of charge carriers.

Note: In metals concⁿ of e⁻ are very high & also they exist with equal distribution & there is no diffusion.

Length of Diffusion:-

$$L = \sqrt{\tau D} \quad \text{cm.}$$

but $D = \frac{1}{2} u v_T$

$$L = \sqrt{\frac{1}{2} u v_T \tau} \quad \text{cm.}$$

$\tau \rightarrow$ carrier lifetime
 $\tau \rightarrow$ Average life

* carrier lifetime is average lifetime

* Length of Diffusion is average length.

* Length of Diffusion depends on diffusion constant, carrier lifetime mobility of charge carriers & tempⁿ.

e⁻ Diffusion length $L_n = \sqrt{D_n \tau_n}$ cm.

holes " " $L_p = \sqrt{D_p \tau_p}$ cm.

$\tau_n \neq \tau_p$

e⁻ Diffusion current density [$J_n(\text{diff})$]:-

$J_n(\text{diff}) = +q D_n \frac{dn}{dx} \text{ A/cm}^2$

hole Diffusion Current density [$J_p(\text{diff})$]:-

$J_p(\text{diff}) = -q D_p \frac{dp}{dx} \text{ A/cm}^2$

e⁻ Diffusion Current $I_n(\text{diff}) = J_n(\text{diff}) \times \text{Area}$

hole Diffusion current $I_p(\text{diff}) = J_p(\text{diff}) \times \text{Area}$

• If Area is not specified in the problem then by default always Consider unit cross sectional area.

Total current density in a semiconductor

$$J = J_n + J_p$$

$$J_n = (J_n)_{\text{drift}} + (J_n)_{\text{diff}}$$

$$= nq \mu_n E + q D_n \frac{dn}{dx}$$

$$J_p = (J_p)_{\text{drift}} + (J_p)_{\text{diffusion}}$$

$$= p q \mu_p E - q D_p \frac{dp}{dx}$$

$$J = \underbrace{qn \mu_n E}_{(J_n)_{\text{drift}}} + \underbrace{q D_n \frac{dn}{dx}}_{(J_n)_{\text{diffusion}}} + \underbrace{q p \mu_p E}_{(J_p)_{\text{drift}}} - \underbrace{q D_p \frac{dp}{dx}}_{(J_p)_{\text{diffusion}}}$$

$$J = q n \mu_n E + q p \mu_p E + 2 D_n \frac{dn}{dx} - q D_p \frac{dp}{dx}$$

* Drift current depends on carrier concentration, mobility of charge carriers & field intensity.

* Drift current mainly depends on electric field intensity

* Diffusion current mainly depends on concentration gradient.

Operating Temperatures

• for Ge

-60°C to +75°C

Maximum operating temperature = 75°C.

• for Si

-60°C to 175°C

Maximum operating temperature = 175°C

→ Normal Working temperature:-

100k to 400k

Leakage Currents (I_0):-

* This is also called as reverse saturation current or minority carrier current.

* It is also called as temperature generated or thermally generated current.

* It never depends on applied voltage across the material.

* This current is saturated wrt voltage only. when we will increase voltage the current will not vary (saturates).

* It increases with increase in temperature.

* For 1°C rise in temperature, the value of current (I_0) increase by 7%.

* I_0 gets doubled by increasing 10°C of temperature in both Ge & Si.

$$I_0 = I_0 \cdot 2^{\frac{(T_2 - T_1)}{10}}$$

Ge	Si
$I_0 \approx 1 \mu A$	$I_0 \approx nA$

I_0 of Ge > I_0 of Si

* I_0 depends on minority carriers and minority carrier concentration will be depending on temperature. Hence this current is generated only because of temp^r. hence called thermally generated current.

* It is highly sensitive to temp^r.

* For better performance leakage currents must be smaller.

if leakage currents are small the temperature effect on the material or device will be small & this indicates better thermal stability.

* Si is having better thermal stability than Ge.

* The greatest advantage of Si is smaller leakage currents.

Conductivity Sensitivity:-

1. In intrinsic semiconductor, conductivity increases with the temperature.

for 1°C rise in Ge, σ ↑ by 6%.

for 1°C rise in Si, σ ↑ by 8%.

2. when compared to Ge, Si is having higher sensitivity to the temperature but Si is more suitable for high temperature application & this is due to the smaller leakage currents.

Electrical Properties of Ge & Si

↓ Properties	Ge	Si
1. Atomic Number	32	14
2. Total no. of Atoms (Density of atoms)	$4.421 \times 10^{22} / \text{cm}^3$	$5 \times 10^{22} / \text{cm}^3$
3. Intrinsic Concentration (n_i) _{300K} (atom/cm ³)	2.5×10^{13}	1.5×10^{10}
4. Intrinsic Resistivity ρ_i (300K) (Ωm-cm)	45	2,30,000
5. Leakage Current (I_0)	$\approx 1 \mu A$	$\approx nA$
6. Max ^m operating Temp ^r	75°C	175°C
7. Power handling Capability	low power	High power

* when compare to Ge, Si. is more

preferable due to

[a] Smaller leakage Current.

[b] High temperature application.

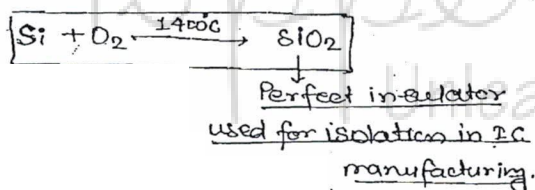
[c] High power handling

[d] Si is plenty available on the surface of earth \rightarrow This is the primary reason why silicon is widely used by semiconductor's device manufacturer's.

[e] Si is very cheap & economical.

[f] Favourable property to form SiO_2 .

\downarrow
 This is the main reason why Si is very fancy for IC manufacturing.



Major Disadvantage of Silicon:-

* Smaller Conductivity than Ge.

Note:- Silicon when exposed to 1400°C will melt & we get liquid Silicon & when reacted with the oxygen we get SiO_2

SiO_2 is a perfect insulator.

SiO_2 is used to provide isolation in between the components during the IC manufacturing.

Minimum Conductivity in Semiconductor

The conductivity of a semiconductor

is

$$\boxed{\sigma = nq\mu_n + pq\mu_p} \quad \text{--- (i)}$$

By mass action law we can write

$$p = \frac{n_i^2}{n} \quad \text{--- (ii)}$$

Substituting (ii) in eqⁿ (i)

$$\sigma = nq\mu_n + q\mu_p \cdot \frac{n_i^2}{n} \quad \text{--- (iii)}$$

differentiating above equation w.r.t n

$$\frac{d\sigma}{dn} = q\mu_n + q\mu_p n_i^2 \left(-\frac{1}{n^2}\right)$$

$$\frac{d^2\sigma}{dn^2} = q\mu_p n_i^2 \left(\frac{2}{n^3}\right)$$

since second derivative is positive we get the condition for minimum conductivity by $\frac{d\sigma}{dn} = 0$

$$q\mu_n + q\mu_p n_i^2 \left(-\frac{1}{n^2}\right) = 0$$

$$\mu_n = \mu_p \cdot (n_i)^2 \left(\frac{1}{n^2}\right)$$

$$n^2 = \frac{\mu_p}{\mu_n} \cdot (n_i)^2$$

$$\boxed{n = n_i \sqrt{\frac{\mu_p}{\mu_n}}} \quad \text{--- (iv)}$$

Putting this value in eqⁿ (i)

$$\sigma = n_i q \sqrt{\mu_n \mu_p} + q\mu_p \frac{n_i^2}{n_i \sqrt{\frac{\mu_p}{\mu_n}}}$$

$$\sigma = n_i q \sqrt{\mu_n \mu_p} + q n_i \sqrt{\mu_n \mu_p}$$

$$\boxed{\sigma = 2n_i q \sqrt{\mu_n \mu_p}} \quad \text{--- (v)}$$

eqⁿ (v) is the equation to calculate the minimum conductivity.

By eqⁿ (v) + eqⁿ (ii)

$$P = n_i \sqrt{\frac{\mu_n}{\mu_p}}$$

$$\sigma_{\min} = 2q n_i \sqrt{\mu_n \mu_p}$$

Question: If drift velocity of holes under a field gradient of 100 V/m is 5 m/sec find its mobility

Solution:

$$\mu = \frac{v_d}{E} = \frac{5}{100} = 0.05 \text{ cm}^2/\text{V-sec}$$

Question: The carrier mobility in a semiconductor is 0.4 m²/V-s if diffusion constant at room temp^r is _____

$$D = \mu V_T$$

$$= 0.4 \times 0.026$$

$$D = 0.0104 \text{ m}^2/\text{sec}$$

Q The minority carrier lifetime & diffusion constant in a SC material are 100 μsec & 100 cm²/sec respectively the diffusion length of charge carrier is

Solution

$$L = \sqrt{D \tau}$$

$$= \sqrt{100 \times 10^{-4} \times 100}$$

$$L = 1 \text{ cm} \text{ Answer}$$

Question: A flat aluminium strip of a resistivity of $3.44 \times 10^{-8} \Omega \text{ m}$, a cross sectional area of $2 \times 10^{-4} \text{ m}^2$ & a length of 5 mm. is subject to a current flow of 50 mA. find voltage drop across the bar

Solution:

$$V = I \cdot R$$

$$= 50 \times 10^{-3} \times 3.44 \times 10^{-8} \times \frac{5 \times 10^{-3}}{2 \times 10^{-4}}$$

$$= 50 \times 3.44 \times 2.5 \times 10^{-9}$$

$$= 125 \times 3.44 \times 10^{-4} \text{ volt}$$

$$= 43 \text{ mV}$$

Question A SC wafer (having negligible thickness) is 0.5 mm thick. a potential of 100 mV is applied across the thickness

(a) what is the drift velocity if mobility is 0.2 m²/V-sec

(b) How much time is required for an electron to move across the thickness

Solution:

$$(a) E = \frac{V}{d} = \frac{100}{0.5} = 200 \text{ V/m}$$

$$v_d = \mu E = 0.2 \times 200 = 40 \text{ m/sec}$$

$$(b) t = \frac{0.5 \times 10^{-3}}{40} = 1.25 \times 10^{-5}$$

$$t = 12.5 \mu\text{sec}$$

Question: A small concentration of minority carriers are injected into a homogeneous SC crystal at one point & having an electric field E

In N-type SC

$$N_A = 0$$

$$n \approx N_D + P \quad \text{or} \quad n \approx N_D$$

or

$$n \approx N_D$$

* N_D is called donor concentration or the density of donor atoms & it represents the no. of pentavalent atoms added to the SC.

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$$N_D = \text{Total no of atoms/cm}^3 \times \text{Impurity ratio}$$

* In N-type SC free e^- concentration is approximately equal to N_D (the density of donor atoms).

* In N-type SC, the current is predominantly dominated by the flow of electrons.

* The conductivity of entire SC is

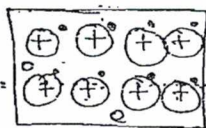
$$\sigma_N = nq\mu_n + pq\mu_p \quad \Omega/\text{cm.}$$

$$\approx nq\mu_n \quad \Omega/\text{cm.}$$

$$\sigma_N \approx N_D q \mu_n \quad \Omega/\text{cm.}$$

The conductivity due to minority carrier is almost negligible.

entire SC is represented as



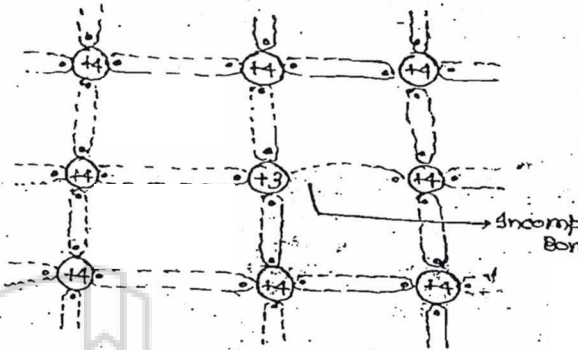
(+) ion \rightarrow it is a neutral atom with 1e⁻ less.

* ions are called immobile charge particles.

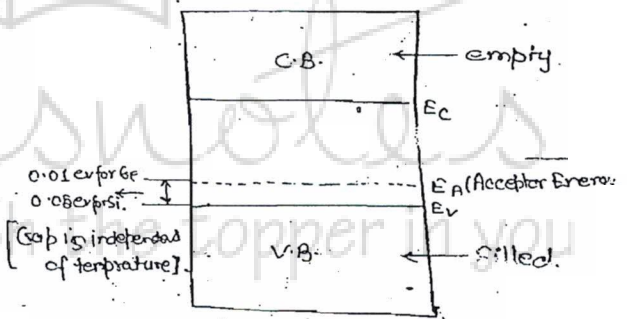
P-Type Semiconductor or Acceptors:-

* The impurity is trivalent.

Crystalline structure at 0°K.



Energy Band Diagram at 0°K.

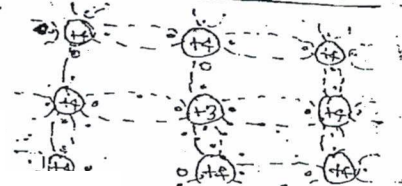


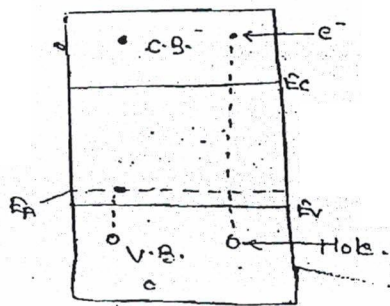
* Acceptor energy level is a discrete energy level created just above the valence band.

* Acceptor energy level denotes the energy level of trivalent atoms to the SC.

* P-type SC at 0°K will be working as an insulator.

Crystalline structure at 300°K.





Energy Band Diagram at 300K:

- * In p-type SC every impurity atom will be receiving $1e^-$ to complete its bonding hence p-type is also called as acceptor.
- * $P \gg n$.
- Majority carriers are holes, minority carriers are e^- .
- * when p-type SC is placed at room temperature, because of thermal energy a large no. of covalent bonds will be broken & equal no. of electrons & holes are generated most of these e^- 's will be moving into acceptor energy level to complete the bonding's & very few e^- 's will be moving from valence band to conduction band so that the hole concentration in the V.B. is far greater than e^- concⁿ in the C.B.

* In p-type SC current is mainly due to holes.

* The condition for p-type is

$$P \gg n \quad \text{or} \quad n \ll p$$

the e^- concⁿ is reducing below due to a large no. of bondings.
 * according to the law of electrical neutrality —

$$N_D + P = N_A + n$$

Since $N_D = 0$.

$$P = N_A + n \quad \text{only for IES.}$$

or

$$P \approx N_A \quad \text{for all exams}$$

where N_A = acceptor concentration & it denotes the no. of trivalent atoms added to the SC.

$$N_A = \text{Total no. of atoms/cm}^3 \times \text{Impurity\%}$$

* The conductivity of p-type SC is

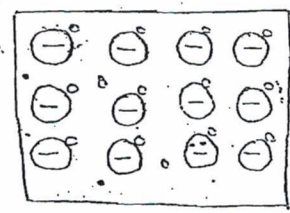
$$\sigma_p = n_e q_e \mu_n + p q_h \mu_p \quad \text{W/cm.}$$

$$\sigma_p \approx N_A q_h \mu_p \quad \text{W/cm.}$$

* The conductivity due to minority carriers is almost negligible.

* N-type SC is superior to P-type because $\mu_n > \mu_p$.

* P-type SC is represented as



LAW OF ELECTRICAL NEUTRALITY

- * Based on law of conservation of charge
- * Total positive charges = Total negative charges