



IES/GATE

←—————→

MECHANICAL ENGINEERING

VOLUME - 6

PRODUCTION ENGINEERING - 2



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Production Engineering – 2

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*PRODUCTION
ENGINEERING-II*

CHAPTER :- 1 THEORY OF METAL CUTTING

Theory of metal cutting

human
air
↓
100 microns

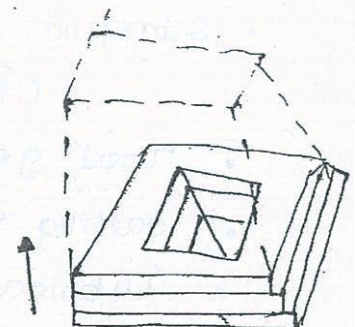
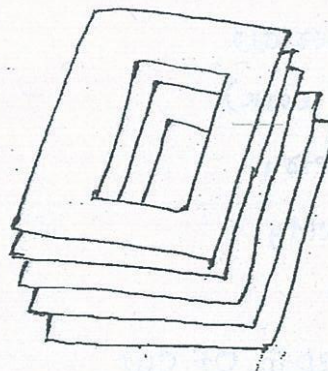
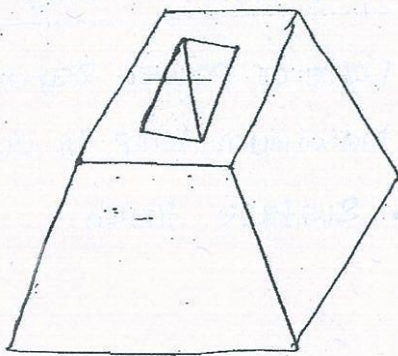
Classification of manufacturing process

- Shaping or forming (zero process)
 ↓
 no change in mass
- Joining process (positive process)
 ↓
 mass of workpiece is more
- Removal process (negative process)
 ↓
 Removal of mass

• Regenerative manufacturing

Regenerative manufacturing

- i) production of solid products in layer by layer from raw materials in different forms.
- ii) Very rapid, accurate and used for Rapid prototyping and tooling.



Advantage:-

(workpiece)

- i) Process is independent of part features.
- ii) No blanks are required
 preformed shape
 Shape
- iii) Toolless process
- iv) Easily Automation possible.

no material
require

used in
Automobile

Machining

- Machining is an eventual process of finishing by which jobs are produced to the desired dimensions and surface finish by gradually removing the excess material from the preformed blank in the form of chips with the help of cutting tools moved past the work surface.
- Machining is a removal process.

Machining aim to

- i) fulfill its functional requirements.
- ii) Improve its performance.
- iii) prolong its service.

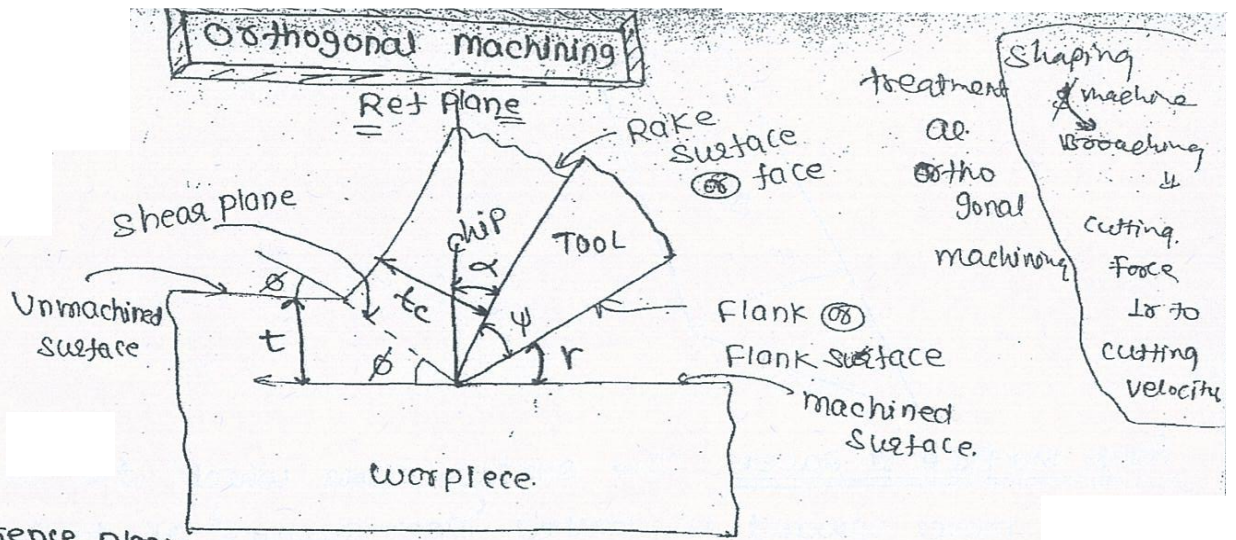
Drawback in Machining

- i) Loss of material in the form of chips

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Q. Name four independent variables and three dependent variables in metal cutting.

Independent variables	Dependent variables
<ul style="list-style-type: none"> • Starting material (tool/work) • Tool geometry • cutting velocity • Lubrication • Feed & Depth of cut 	<ul style="list-style-type: none"> • Force or power requirements • maximum temp in cutting • Surface finish



Reference plane:

is to machined surface at the cutting edge.

α = Rake angle

γ = clearance angle @ relief angle

American system

ϕ = Shear angle

ψ = Lip angle @ cutting angle @ knife angle @ wedge angle

t_c = chip thickness

t = Uncut chip thickness @ undeformed chip thickness.

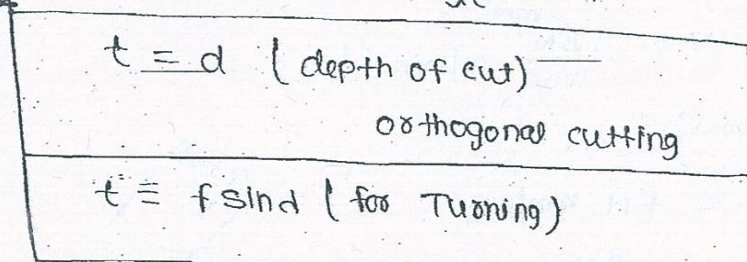
$t_c > t$

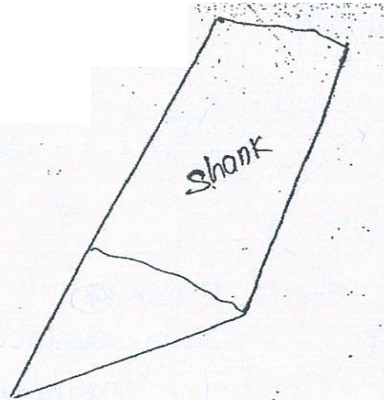
$$\sigma = \frac{t}{t_c} < 1$$

For Brittle material (no shear failure

$t \approx t_c$ (no shear flow
no chip flow)

and $\sigma = \frac{t}{t_c} \approx 1$



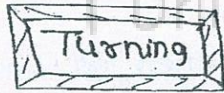


Rack surface or face:- The surface along which the chip moves upward is called 'Rack surface' of tool.

Flank or Relief surface:- the other surface which is relieved to avoid rubbing with the machined surface is called 'Flank' or flank surface.

Rake angle (α):- angle of inclination of rake surface from reference plane i.e. normal to horizontal machined surface.

clearance angle or Relief angle (r):- angle of inclination of clearance or flank surface from the finished surface.



Speed, feed and depth of cut

peripheral velocity

$$V = \pi \cdot \omega$$

$$= \frac{D}{2} \times \frac{2\pi N}{60} = \frac{\pi D N}{60} \text{ m/sec.}$$

$$V = \pi D N \text{ m/min}$$

$$V = \frac{\pi D N}{1000} \text{ m/min.}$$

feed:- f (mm/rev)

$$V_f = f N \text{ mm/min}$$

$$= \frac{f N}{60,000} \text{ m/sec.}$$



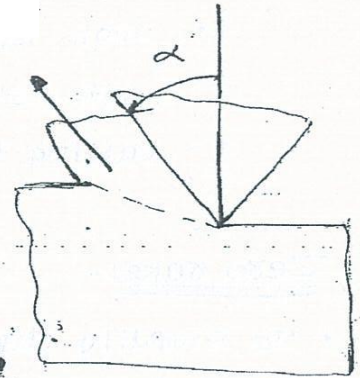
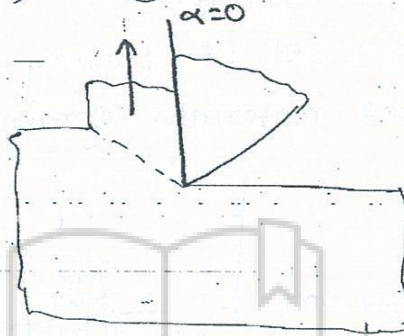
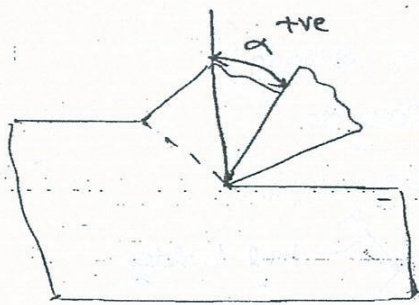
No feed in
orthogonal
cutting

$$D_1 = D_2 + 2d$$

$$d = \frac{D_1 - D_2}{2} = \text{depth of cut (doc)}$$

Discussion on Rack angle

Rack angle can be, +ve, -ve or zero.



positive rake

- Reduce cutting force
- Reduce cutting power

Positive rake angles are recommended
= (tool sharp)

- Machining low strength material.
- Low power machine
- Long shaft of small diameter. (due to low stiffness)
- Set-up lacks strength and rigidity.
- Low cutting speed

cutting tool material: HSS

ductile material

18-4-1

18% W, 4% Cr, 1% V
Rest Fe

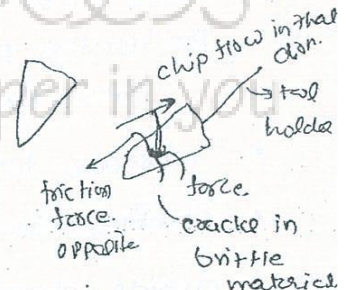
for +ve rake → materials should

HSS tool fail temp above 600° (HSS) be ductile

carbide } 1500 m/min.
ceramic } brittle material
6000 m/min

Negative rake:- (tool dull)

- Increase edge strength (mechanically and thermally)
- increase life of the tool.
- increase the cutting force.



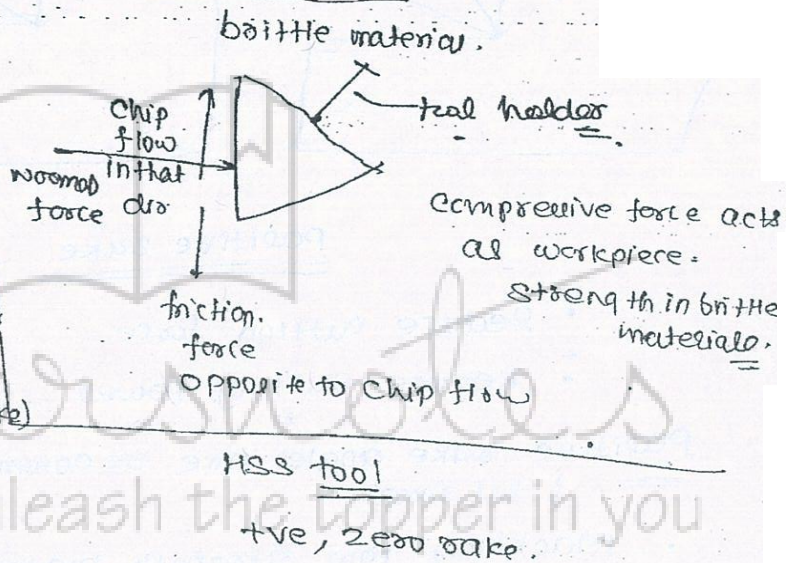
- It requires high cutting speed.
- Requires ample power.
- Heavy impact load.

Negative rake angles are recommended

- Machining high strength alloy.
- High speed cutting.
- with rigid set-up. (every thing strong)
- cutting tool material: Ceramic, Carbide

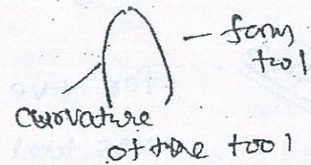
Zero rake:-

- To simplify design and manufacturing of the form shape tools.
- without any manufacturing to get zero rake.
- thread cutting tool (zero rake)
particular profile cut
gear manufacturing

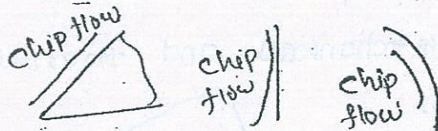


- Increase tool strength.
- complex tool are formed by HSS (broaching, hobbing)
- avoid digging of the tool into the workpiece.
 - +ve rake (digging in there) (inside digging)
 - ve rake (outside digging)
- Broau is turned with zero rake angle.
- cast iron use zero rake angle.

↓ inside Carbon Content more than 2%.
 Carbon Content forms cementite.



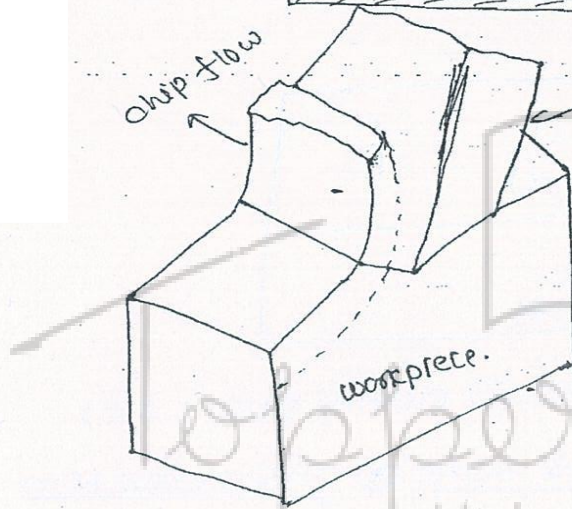
- -ve rake angle: Shear strain is more.



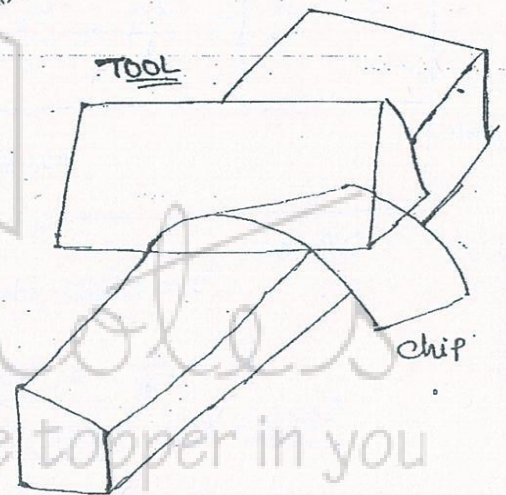
Clearance angle

- Provided to avoid rubbing of the tool (flank) with the machined surface.
- Reduce tool wear.
- Increase tool life.
- must be +ve (3° - 15°)

Types of machining



Orthogonal cutting



Oblique cutting

Orthogonal Cutting:

- Cutting edge of the tool is perpendicular to direction of cutting velocity.
- The cutting edge is wider than the workpiece width and extends beyond the workpiece on either side. Also the width of workpiece is much greater than the depth of cut.
- The chip generated flows on the rake face of the tool with chip velocity perpendicular to cutting edge.
- The cutting forces act along two directions only.

NOTE

During cutting of metal, an increase in cutting speed cutting force to remain unaffected and slightly reduce.

But Power, chip production and temperature will increase.

∴ cutting speed increases it causes
 → cutting forces to remain Unaffected.

∴ more ~~more~~ heat more temp of workpiece more.
 reduce the cutting force.

Shear angle (ϕ)

by definition.

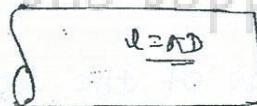
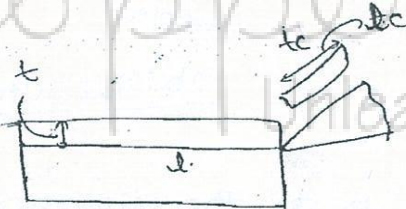
$\delta = \frac{t}{t_c} = \frac{dc}{l} = \frac{vc}{v} = \frac{\sin \phi}{\cos(\phi - \alpha)} = \frac{1}{h}$
$\tan \phi = \frac{\delta \cos \alpha}{1 - \delta \sin \alpha}$

Where

δ = chip thickness ratio @ cutting ratio ; $\delta < 1$

$h = \frac{1}{\delta}$ = Inverse of chip ratio @ chip reduction

factor @ chip Compression ratio ; $h > 1$



$dc = 100 \text{ mm}$

$\delta = \frac{dc}{l} = \frac{100}{100}$

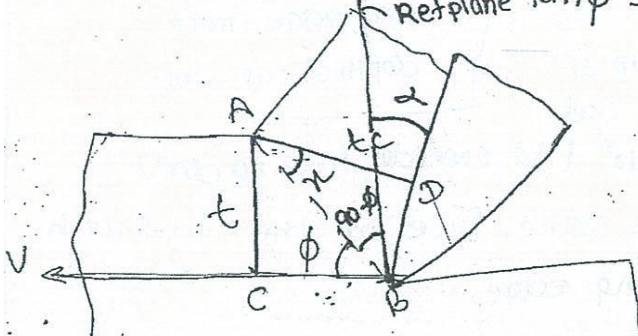
* If $\alpha = 0$

$\tan \phi = \frac{\delta \cos 0^\circ}{1 - \delta \sin 0^\circ} = \delta$
--

IAS-2009 main

∴

Prove that
 Retplane $\tan \phi = \frac{\delta \cos \alpha}{1 - \delta \sin \alpha}$



$$\frac{t}{AB} = \sin\phi$$

$$\boxed{t = AB \sin\phi} \quad \text{--- (i)}$$

$$\frac{t_c}{AB} = \cos\alpha$$

$$\boxed{t_c = AB \cos\alpha}$$

$$\boxed{t_c = AB \cos(\phi - \alpha)} \quad \text{--- (ii)}$$

$$\angle B = 90 - \phi + \alpha$$

$$\angle A + \angle B + \angle D = 180^\circ$$

$$\alpha + 90 - \phi + \alpha + 90 = 180^\circ$$

$$\alpha = \phi - \alpha$$

$$\gamma = \frac{t}{t_c} = \frac{AB \sin\phi}{AB \cos(\phi - \alpha)}$$

$$\sin\phi = \gamma \cos(\phi - \alpha)$$

$$\sin\phi = \gamma [\cos\phi \cdot \cos\alpha + \sin\phi \sin\alpha]$$

$$\sin\phi (1 - \gamma \sin\alpha) = \cos\phi \cdot \gamma \cos\alpha$$

$\tan\phi = \frac{\gamma \cos\alpha}{1 - \gamma \sin\alpha}$	$\gamma = \frac{\sin\phi}{\cos(\phi - \alpha)}$
--	---

$$\alpha = 12^\circ$$

$$\gamma = \frac{0.81}{1.8} = 0.45$$

$$\phi = \tan^{-1} \left[\frac{0.45 \cos 12^\circ}{1 - 0.45 \sin 12^\circ} \right]$$

$$= 26^\circ$$

cutting shear strain (ϵ)

$\epsilon = \cot\phi + \tan(\phi - \alpha)$
$\epsilon = \frac{\cos\alpha}{\sin\phi \cos(\phi - \alpha)}$

$$\epsilon = \cot \phi + \tan(\phi - \alpha)$$

$$= \frac{\cos \phi}{\sin \phi} + \frac{\sin(\phi - \alpha)}{\cos(\phi - \alpha)}$$

$$= \frac{\cos \phi \cdot \cos(\phi - \alpha) + \sin \phi \cdot \sin(\phi - \alpha)}{\sin \phi \cdot \cos(\phi - \alpha)}$$

$$\epsilon = \frac{\cos \alpha}{\sin \phi \cos(\phi - \alpha)}$$

$$\epsilon = \cot \phi + \tan(\phi - \alpha)$$

negative back

* If $\alpha = 0$

$$\epsilon = \cot \phi + \tan \phi \geq 2$$

$$= \overset{a}{x} + \overset{b}{\frac{1}{x}} \text{ form}$$

A.M \geq G.M

$$\frac{x + \frac{1}{x}}{2} \geq \sqrt{x \cdot \frac{1}{x}}$$

* $x + \frac{1}{x} \geq 2$

chip flow
Shear
Strain
max.

* If $\alpha = 0$, $\epsilon \geq 2$
 $\epsilon_{\min} = 2$ when $\phi = 45^\circ$

$$\frac{d\epsilon}{d\phi} = -\cot \phi \csc^2 \phi + \sec^2(\phi - \alpha) = 0$$

$$\phi = 90^\circ$$

$$\alpha = 12^\circ$$

theoretically minimum possible Shear Strain to occur.

$$\epsilon = \cot \phi + \tan(\phi - 12)$$

$$\frac{d\epsilon}{d\phi} = -\cot \phi \csc^2 \phi + \sec^2(\phi - 12) = 0$$

(P1)
GATE-1990
|||

$$\cos^2 \phi = \sec^2 (\phi - 12)$$

$$\cos^2 (\phi - 12) = \sin^2 \phi$$

$$\Rightarrow \sin \phi = \cos (\phi - 12)$$

$$\sin \phi = \cos \phi \cdot \cos 12 + \sin \phi \cdot \sin 12$$

$$\sin \phi (1 - \sin 12) = \cos \phi \cdot \cos 12$$

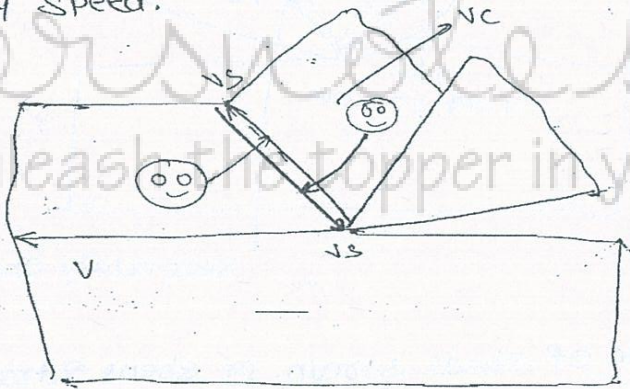
$$\tan \phi = \frac{\cos 12}{1 - \sin 12} \quad \phi = 51$$

$$\epsilon_{\min} = \cot (51) + \tan (51 - 12)$$

$$= 1.619$$

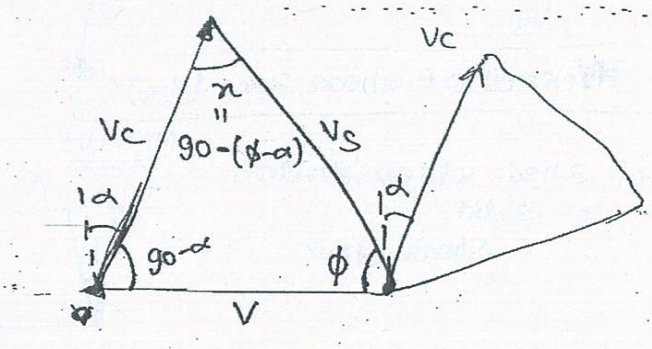
Velocities in metal cutting

- i) The velocity of the tool relative to the work piece (v) is called the cutting speed.
- ii) The velocity of the chip relative to the work, v_s is called the shear velocity.
- iii) the velocity of the chip relative to the tool, v_c is called chip velocity.



ESE-04

Q. Derive the expression for velocities in metal cutting



$$\frac{V}{\sin\{90 - (\phi - \alpha)\}} = \frac{V_c}{\sin\phi} = \frac{V_s}{\sin(90 - \alpha)}$$

this eqⁿ satisfied then resultant is zero.

$$\frac{V}{\cos(\phi - \alpha)} = \frac{V_c}{\sin\phi} = \frac{V_s}{\cos\alpha}$$

$$\frac{V_c}{V} = \frac{\sin\phi}{\cos(\phi - \alpha)} = \delta$$

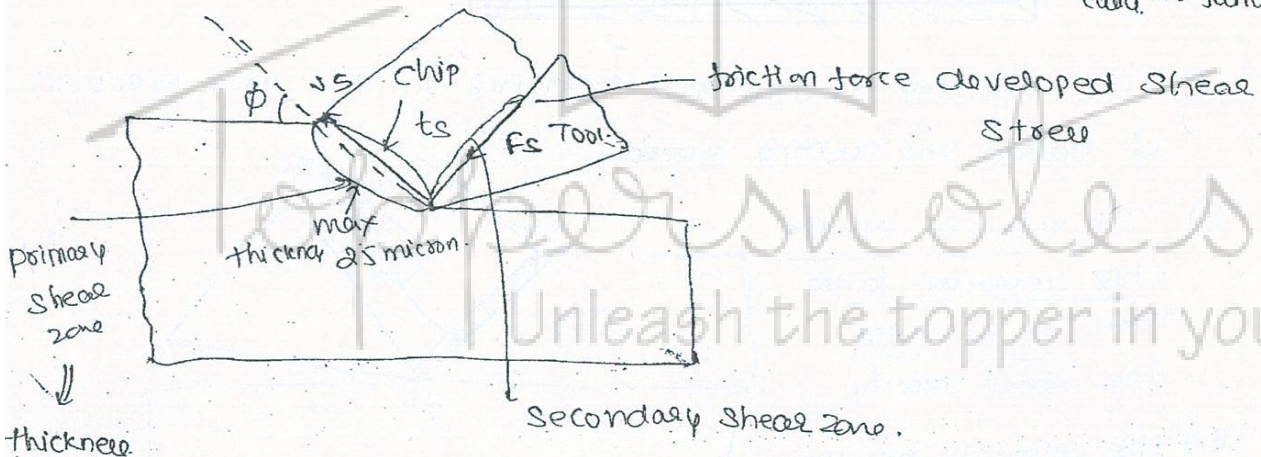
$$\frac{V_s}{V} = \frac{\cos\alpha}{\cos(\phi - \alpha)}$$

$$\tan\phi = \frac{\delta \cos\alpha}{1 - \delta \sin\alpha}$$

Shear plane

thickness zero.

Pract. calcu. No failure



Rate of Shear strain or Shear Strain Rate.

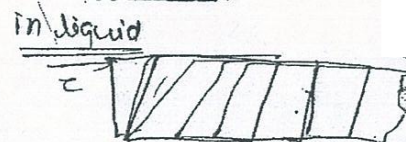
Note:- (It is not shear strain it is rate of shear strain i.e flow)

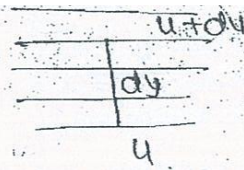
$$\dot{\epsilon} = \frac{d\epsilon}{dt} = \frac{V_s}{\text{thickness of shear zone } (t_s)}$$

if shear stress ~~is~~ acts
 in solid
 Shear strain.



in liquid
 rate of shear strain.





$$\frac{V_s}{t_s} = \frac{du}{dy} = \text{rate of shear strain}$$

⇒ Thickness of shear zone can be taken as $\frac{1}{10}$ th (10%) of shear plane length and its max value is 25 micron.

GATE-2012
ii.

$$\sigma = 0.9$$

$$\alpha = 10^\circ$$

$$V_a = 2.5 \text{ m/s}$$

$$t_s = 25 \text{ micron}$$

$$\tan \phi = \frac{\sigma \cos \alpha}{1 - \sigma \sin \alpha}$$

$$\phi = 22.999$$

$$\phi = \frac{V_s}{t_s} = \frac{V_a}{\cos(\phi - \alpha)} = \frac{V_s}{\cos \alpha}$$

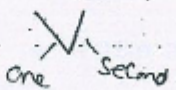
$$= \frac{2.5261}{25 \times 10^{-6}} \Rightarrow \frac{2.5}{\cos(10)} = \frac{V_s}{\cos(10)}$$

$$= 1.01 \times 10^5 \quad V_s = 2.5261$$

Geometry of single point turning tool

cutting edge.

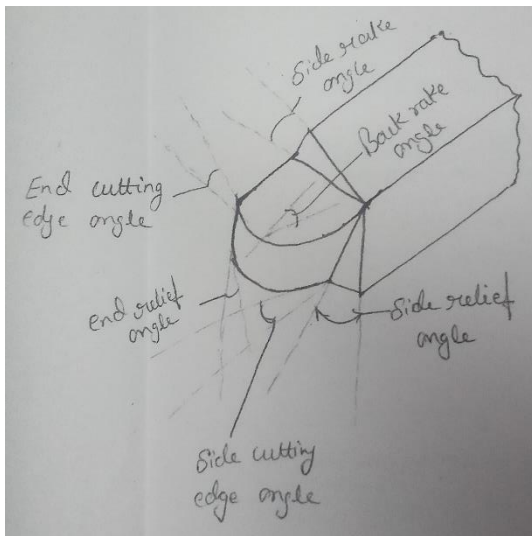
classification:- (A/c to the no of major cutting edges (points) involved)

- Single point:- turning, shaping, planing, slotting tools, parting tools etc.
- Double point:-
 - drilling tools
 - two cutting edge
 - double point 
- Multipoint:- milling, broaching, hobbing tools, saw, grinding wheel etc.
 gear used cut

Machining: -

Metal Removal Process

Single Point Cutting



Multipoint Cutting

(It is a tool with 'n' no of single Point cutting tool)

Single point cutting tool geometry

Steel \rightarrow (0.1-2.1) % of 'c'

H.S.S

T- Series

w- Red hot hardness,

Absorbs ion resistance

Cr- corrosion resistance

V- Harder ability, Shock & wear resistance

M- Series

$M_o \rightarrow$ same as 'w' creep resistance