



# IES/GATE

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## MECHANICAL ENGINEERING

VOLUME - 7

**THEORY OF MACHINE (TOM), POWER PLANT  
ENGINEERING, THERMODYNAMIC**



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*Theory  
Of  
Machine*

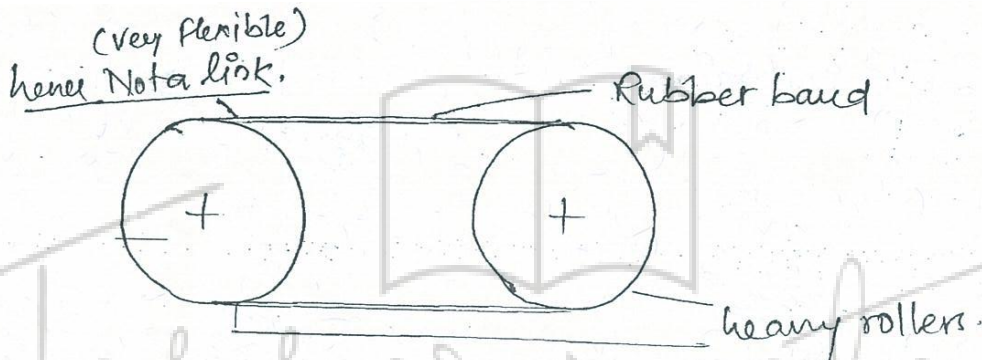


## CHAPTER :- 1 SIMPLE MECHANISM

### Kinematic Link or element :-

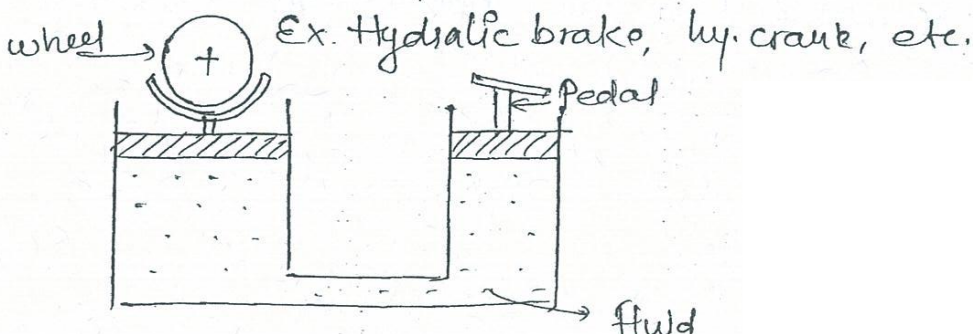
“Every part of a machine which is having some relative motion w.r. to some other part will be known as kinematic link or element.”

It is necessary for the link to be a resistant body so that it is capable of transmitting power and motion from one element to the other element.



### Types of link :-

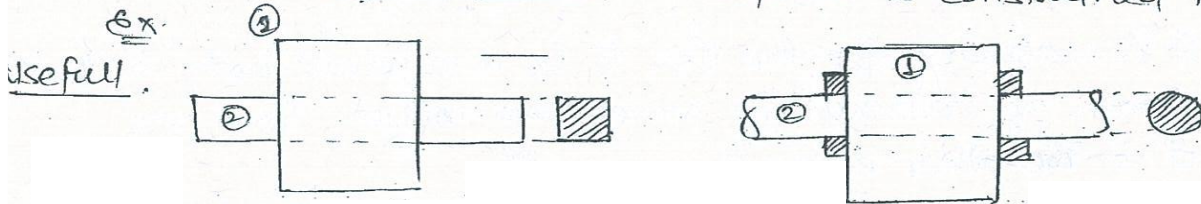
1. Rigid link :- Where deformations are negligible.  
Ex. Crank, connecting rod, piston etc.
2. Flexible link :- Deformations are there but within the permissible limit.  
Ex. Belt drive, Rope drive, chain.
3. Fluid link :- when the power is transmitted because of fluid pressure.



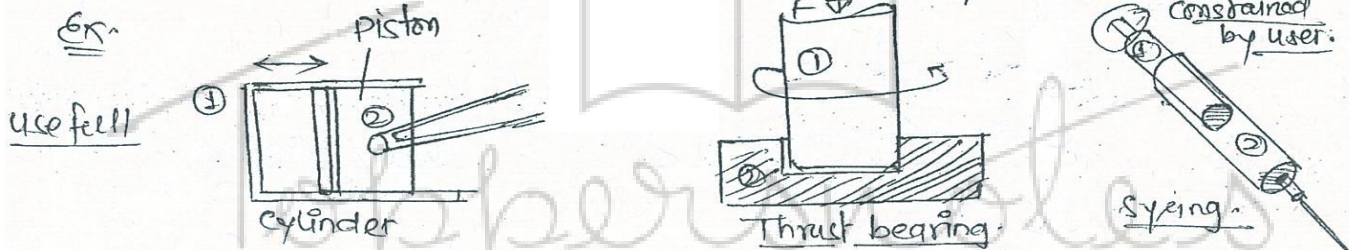
## different types of relative motion :-

for a relative motion - System is having two link.

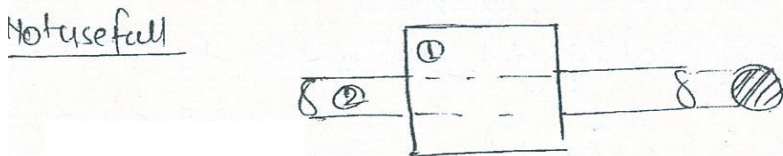
1. Completely constrained motion - Desired motion, where system is constrained itself.  
 [CONSTRAINED]



2. Successfully constrained motion - Motion is constrained by surrounding.  
 [CONSTRAINED]



3. Incompletely constrained motion - unconstrained motion.



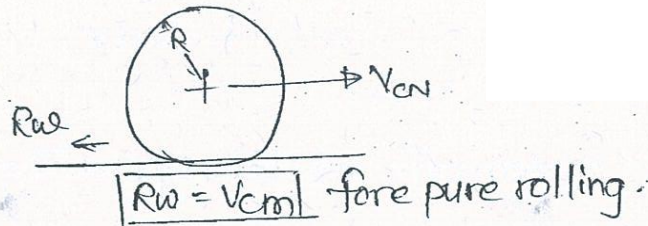
### \* KINEMATIC PAIR :-

"The connection b/w the two links is always a joint or a pair, but this pair will also be a kinematic pair if the relative motion b/w the links is ~~are~~ constrained motion"



(A) According to the type of relative motion :-

- Turning pair (Revolute pair, Pin joint) → Pure turning
- Sliding pair (Prismatic pair) → Pure sliding.
- Rolling pair. → Pure rolling.



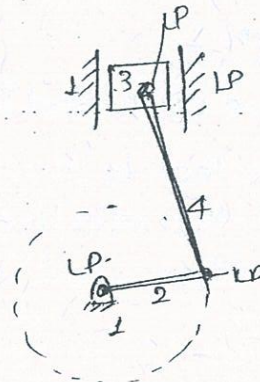
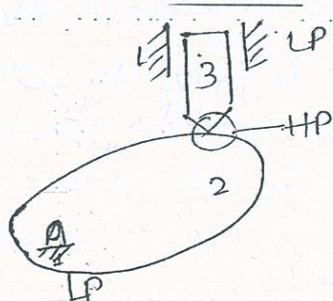
- Screw pair :- Motion over the threads.  
Ex. Nut bolt.
- Spherical pair (Ball in socket joint) - Spherical Motion.  
3D-Rotation.



(B) According to the type of contact :-

- Lower pair - Surface contact.
- Higher pair - Point/Line contact

$1 \text{ HP} = 2 \text{ LP}^*$



- Wrapping pair. Belt pulley, chain sprocket, Rope pulley.

(It is close to higher pair)



according to the type of closure:-

◦ Self closed pair (Closed pair)

→ Permanent contact

◦ forced closed pair

→ forcefully contacted

Ex. - HP in CAM and follower

- Door closers

- Automatic clutch operating system.

Different types of joints:-

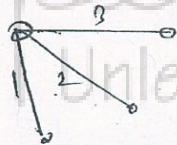
Binary joint

where two links are connected



Ternary joint

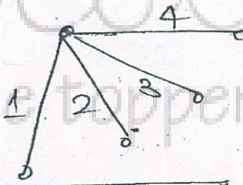
where three links are connected



$$1T = 2B$$

Quaternary joint

where four links are connected

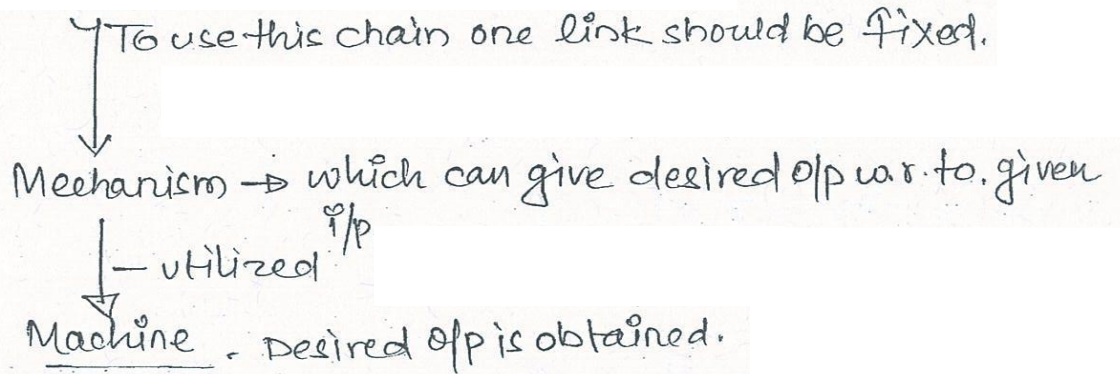


$$1Q = 3B$$

\* KINEMATIC CHAIN :-

"If all the links are connected in such a way such that the 1st link is connected to the last link in order to get the close chain and if all the relative motions in this closed chain are constrained then such a chain is known as kinematic chain."

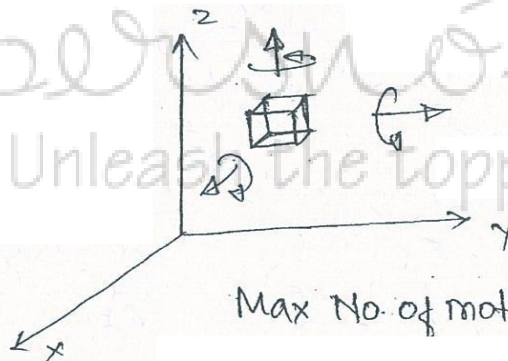
## Kinematic chain:-



### ★ Degree of Freedom (DOF) {Mobility}

“Minimum No. of independent variables required to define the position or motion of the system is known as degrees of freedom of a system”

In 3-D Space





$$\text{Max No. of motion} = 3T + 3R = 6$$

$$\text{DOF} = (6 - \text{Restrained})$$

↳ No. of those motions which are not possible.

Restrains are always b/w of pair.

Pair	Restrains	DOF
	⑤	①
	1T = 1	⑤



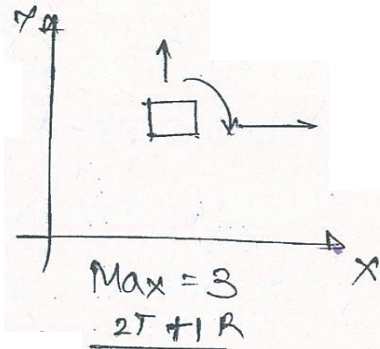
AIM:- To find out DOF of 2-D planar mechanism.

No. of links =  $l$

No. of binary joints =  $j$

No. of higher pairs =  $h$

one link fixed



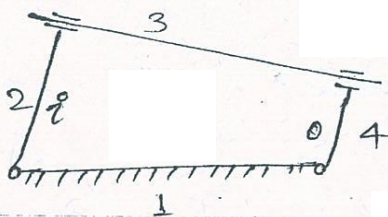
$$F = 3(l-1) - 2j - h$$

Kutzbach's eq<sup>n</sup>

$$F = 3(l-1) - 2j - h - f_r$$

No. of motions which are Not the part of the mechanism.

①

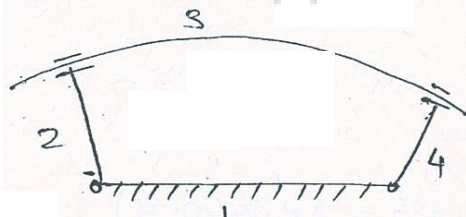


$l=4$   
 $j=4$   
 $h=0$   
 $f_r=1$

$$F = [3(4-1) - 2 \times 4 - 0] - 1$$

$$F = 0$$

②



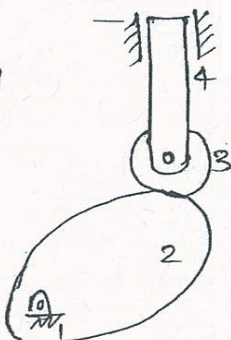
$l=4$   
 $j=4$   
 $h=0$   
 $f_r=0$

$$F = [3(4-1) - 2 \times 4]$$

$$F = 1$$

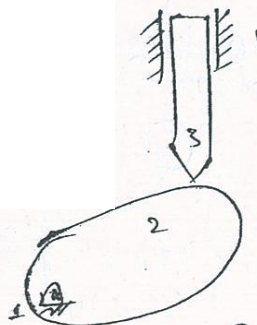
③

$l=4$   
 $j=3$   
 $h=1$   
 $f_r=1$



$$F = 1$$

④



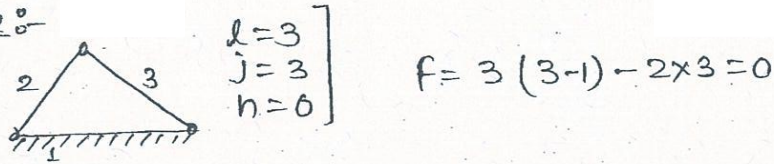
$l=3$   
 $j=2$   
 $h=1$

$$F = 3(3-1) - 2 \times 2 - 1$$

**cases:-**

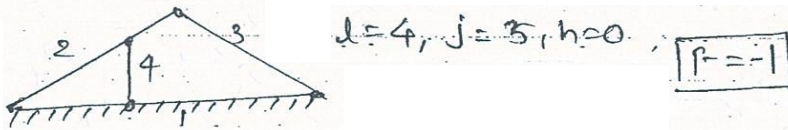
No relative motion  $\rightarrow$  frame/structure

for example:-

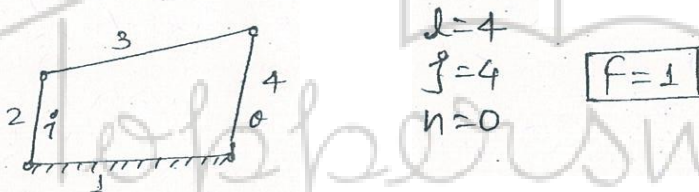


if  $f < 0$   $\rightarrow$  superstructure (indeterminate structure)

for example:

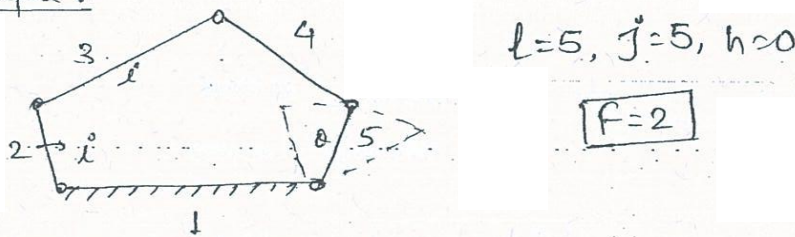


$f = 1$   $\rightarrow$  kinematic chain



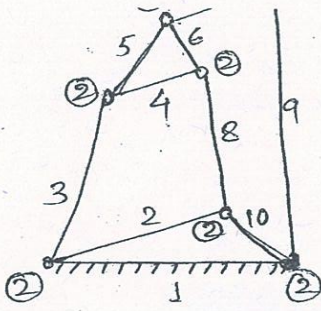
if  $f > 1$  unconstrained chain.

for example:-

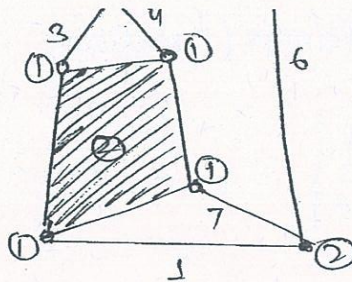


“D.O.F. is the number of inputs required to get the constrained output in a chain.”

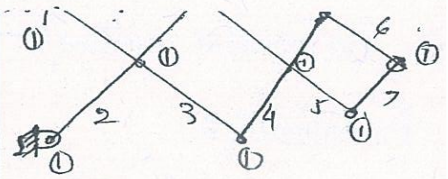




$$\left. \begin{array}{l} l=10 \\ j=13 \\ h=0 \end{array} \right\} \boxed{F=1}$$



$$\left. \begin{array}{l} l=7 \\ j=9 \\ h=0 \end{array} \right\} \boxed{F=0}$$



$$\left. \begin{array}{l} l=8 \\ j=10 \\ h=0 \end{array} \right\} \boxed{F=1}$$

### Spring as a Link. (flexible link)



### Grubler's Equation :-

for those mechanisms in which  $\boxed{F=1}$  &  $\boxed{h=0}$

Applied Kutzbach's equation :-

$$F = 3(l-1) - 2j - h$$

$$1 = 3l - 3 - 2j - 0$$

$$3l - 3 - 2j - 1 = 0$$

$$\Rightarrow \boxed{3l - 2j - 4 = 0}$$

$(3l)$  always - even  
 $l$  always - even.

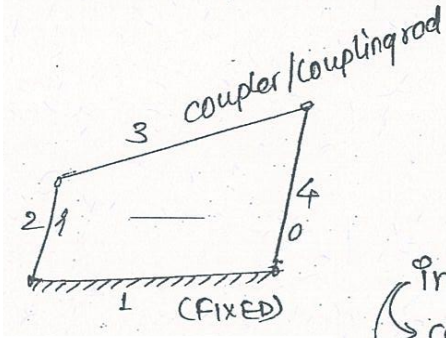
$$\boxed{l_{\min} = 4} \rightarrow$$

1<sup>st</sup> Mechanism  
 with lower pair only  
 ↓  
 SIMPLE Mechanism.

- 4-Bar Mechanism.
- Single slider Mechanism.
- Double slider Mechanism.



(Quadratic cycle Mechanism)



Best position  $\rightarrow$  fixed bcoz it governs  $\left\{ \begin{matrix} \ell/p \\ d/p \end{matrix} \right.$

Input/output  
 $\rightarrow$  complete Rotation - CRANK  
 $\rightarrow$  Partial Rotation - ROCKER  
 (Oscillation)

Inversions:-

Mechanisms which are obtained by fixing one by one different different links.

1. Double crank Mechanism
2. Crank  $\leftrightarrow$  Rocker Mechanism.
3. Double Rocker Mechanism.

Grashof's Law :-

"for the continuous relative motion between the number of links in a mechanism the summation of the lengths of smallest and largest link should not be greater than sum of other two.

for continuous Rotation motion :-

$$(s+l) \leq (p+q)$$

s - shortest link length  
 l - largest link length  
 p, q = other links length.

Best link for rotation = s.

Best position for link = fixed.

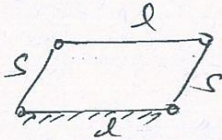
$(s+l) < (p+q)$  Law satisfied :-

- 1 - S - fixed  $\rightarrow$  Double crank.
- 2 - S  $\rightarrow$  Adjacent to fix  $\rightarrow$  crank-Rocker
- 3 - S - Coupler - double rocker.

$(s+l) \leq (p+q)$  law satisfied  
 (Having pair of equal lengths)

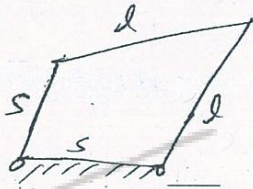
2, 2, s, s

→ Parallelogram linkage :-



s - fixed - double crank  
 l - fixed - double crank.

→ Deltoid linkage :-



s - fixed - crank - rocker  
l - fixed - Crank - rocker

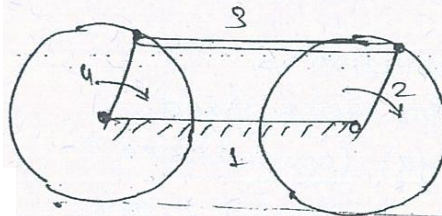
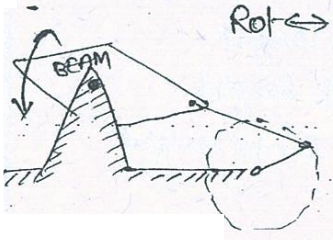
\* If law is not satisfied.  $(s+l) > (p+q)$   
Double Rocker.

PRACTICAL APPLICATIONS OF FOUR BAR MECHANISM :-

1. Beam engine Mechanism.

2. coupling rod of locomotive

Rot ↔ oscillation



Twisting.      Disturb

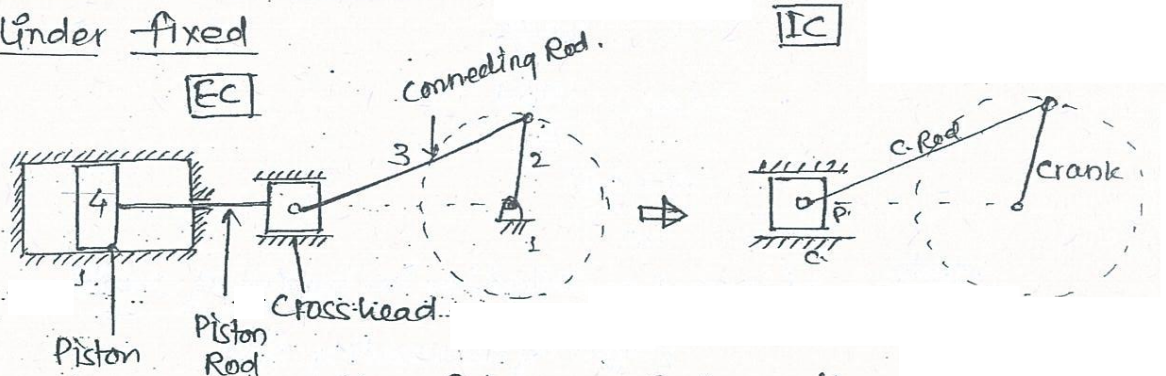


# # single slider crank mechanism

4 Links + 3TP + 1SP

Basic Inversion / 1st Inversion :-

If Cylinder fixed



Rotary ↔ Reciprocating.

If crank fixed :-

II<sup>nd</sup> Inversion

- Whitworth Q.R.M.M
- Rotary IC engine (GINOME ENGINE)

If connecting rod fixed :-

III<sup>rd</sup> Inversion

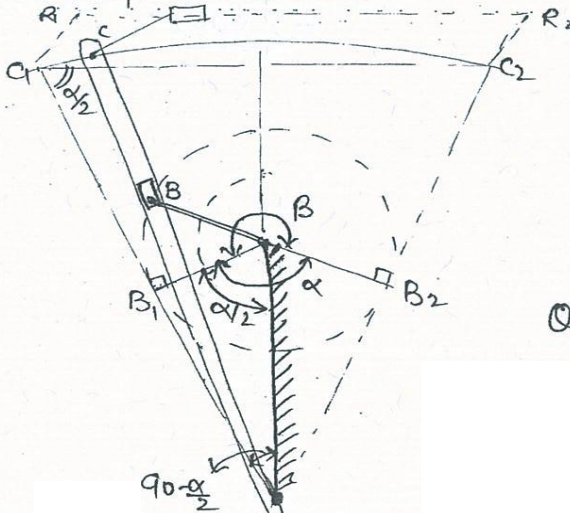
- Crank slotter lever Q.R.M.M
- Oscillating cylinder engine Mechanism.

If slider fixed / piston fixed,

IV<sup>th</sup> Inversion → Hand pump, pendulum pump, Bull engine

★ CRANK AND SLOTTED LEVER Q.R.M.M :-

(connecting rod fixed)



$\beta$  = cutting stroke angle  
 $\alpha$  = Return stroke angle.

$$\alpha + \beta = 360^\circ$$

$$\alpha < \beta$$

Quick return ratio =  $\frac{\beta}{\alpha} = \text{always} > 1$

rotation -  
 oscillation  
 crank - rocker  
 motion

$$\begin{aligned}
 \text{Stroke} &= R_1 R_2 \\
 &= GC_2 \\
 &= 2(C_1M) \\
 &= 2(AE) \cdot \cos\alpha/2 \\
 &= 2(AE) \cdot \frac{(OB_1)}{OA} \\
 &= \frac{2(AE)(OB)}{OA}
 \end{aligned}$$

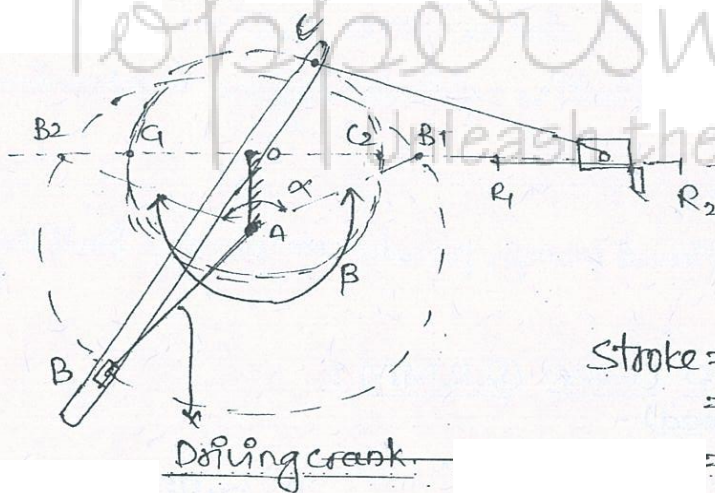
$$\text{Stroke} = \frac{2(\text{length of slotted bar}) \times (\text{length of crank})}{\text{length of connecting Rod.}}$$

\* Whitehat ORMM

Quick Return Ratio (QRR) :-

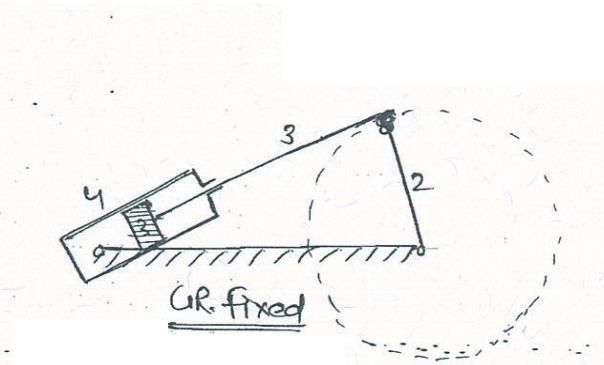
$$\frac{(\text{time})_{\text{cutting}}}{(\text{time})_{\text{return}}} = \frac{\beta}{\alpha}$$

(Always > 1)



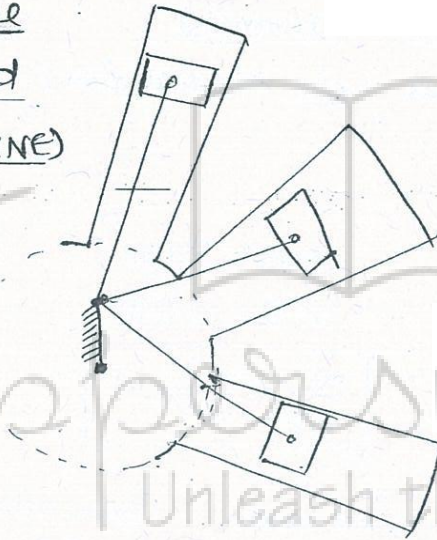
$$\begin{aligned}
 \text{Stroke} &= R_1 R_2 \\
 &= GC_2 \\
 &= \underline{\underline{2(C_1C_2)}}
 \end{aligned}$$

## # cylinder engine mechanism:-



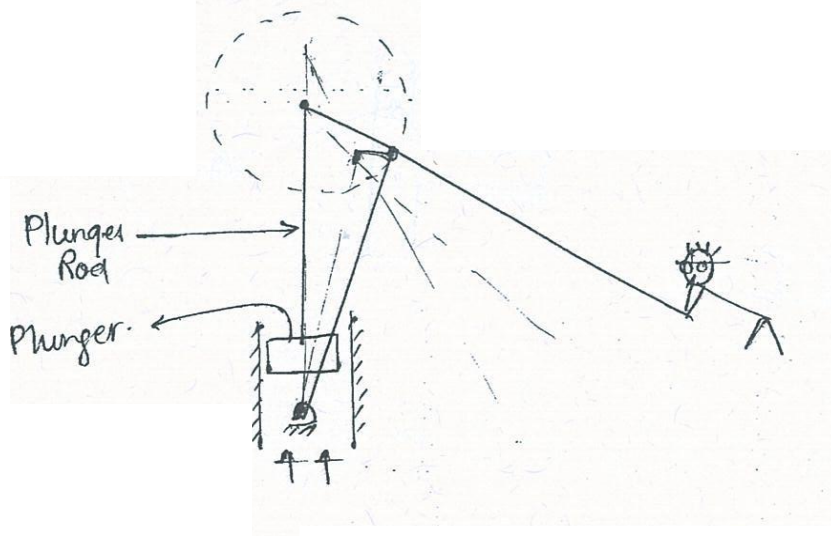
rotary - oscillation  
crank - rockers

★ Rotary IC engine  
Crank fixed  
(GINOME ENGINE)



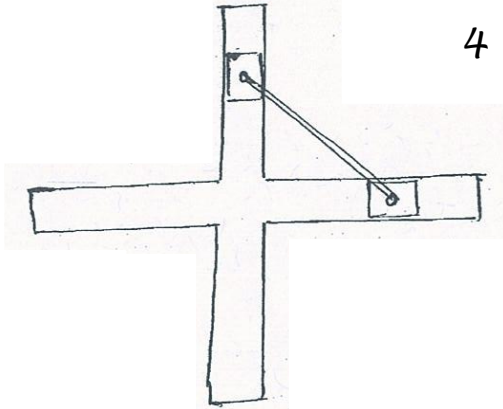
when combustion takes place inside the cy.  
 ↓  
 Input force comes on piston  
 ↓  
 This force will be transmitted to C.R.  
 ↓  
 C.R. & Piston both rotate  
 ↓  
 Cy. block rotates (O/P)

★ Hand pump:-





# # double slider crank mechanism

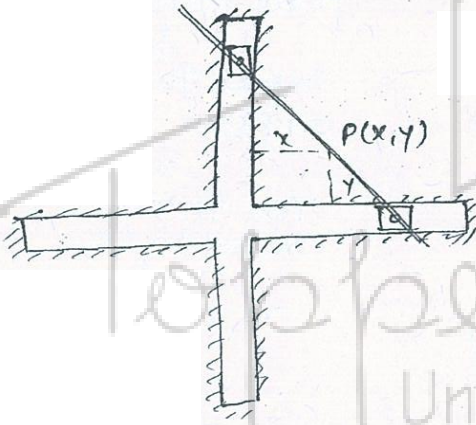


4 link + 2tp + 2sp

tp - turning pair  
sp - sliding pair

## 1. Slotted plate fixed (Elliptical Trammels)

(Sutcliffe yoke Mechanism)



$$\cos \theta = x/AP$$

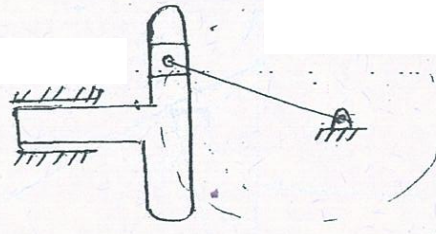
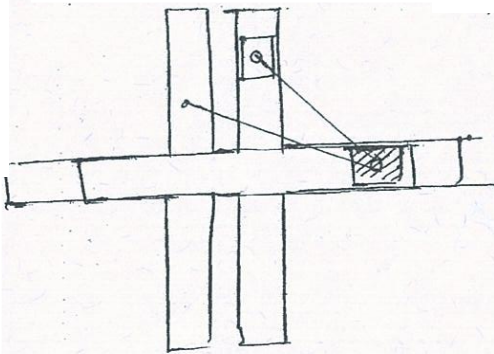
$$\sin \theta = y/BP$$

$$\frac{x^2}{AP^2} + \frac{y^2}{BP^2} = 1$$

Semimajor  
AP

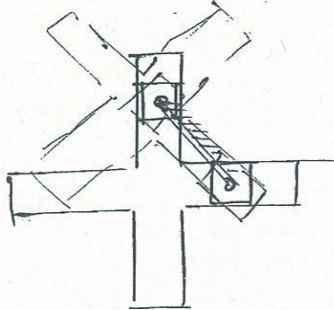
Semiminor  
BP

## 2. Any of slider is fixed:



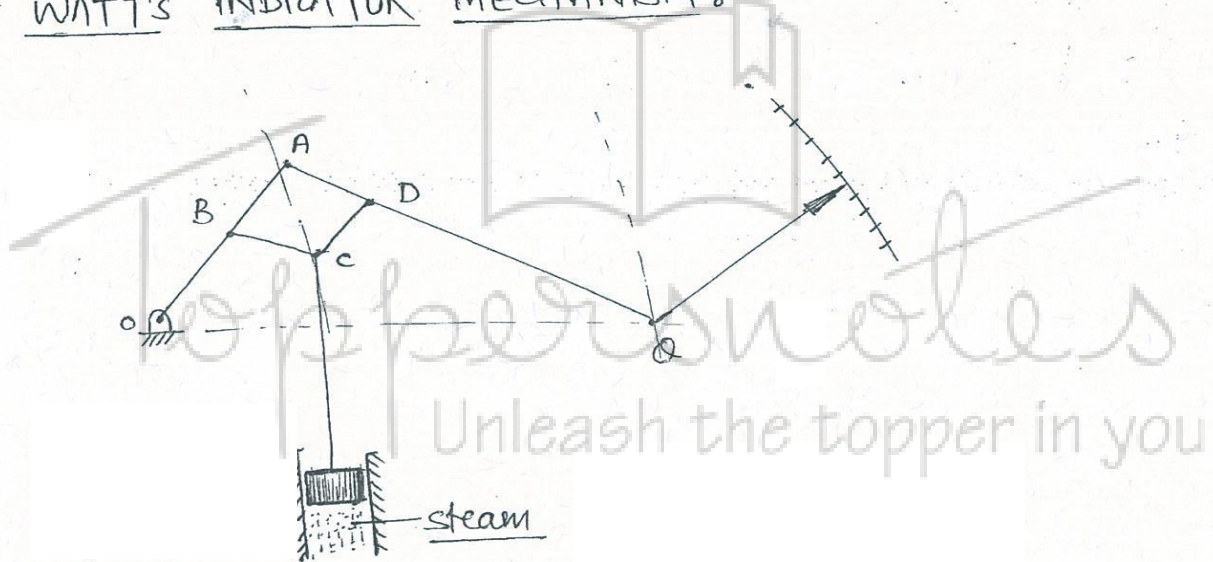
if link connecting slider is fixed.

Oldham's coupling.



Used to connect the shafts having lateral misalignment.

WATT'S INDICATOR MECHANISM :-



Observations:-

- Point c and point Q both move in appx straight line  
 → Apprx ct. Line motion Mechanism.
- There is No relative motion b/w link BC & link CD.  
 → BCD - one link.
- Link BCD } - Levers  
 Link AQ }  
 double lever Mechanism.