



NEET - UG

NATIONAL TESTING AGENCY

Physics

Volume - 2



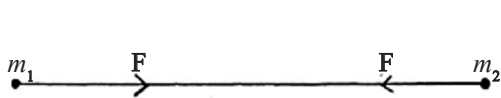
Contents

1. Gravitation	1
2. Mechanical Properties of Solids	20
3. Mechanical Properties of Fluids	34
4. Wave Motion	71
5. Sound Wave	110
6. Thermal Expansion	143
7. Thermodynamics	192

GRAVITATION

Newton's Law of Gravitation:

- * It states that every particle in the universe attracts all other particles with a force which is proportional to the product of their masses and inversely proportional to the square of the distance between them.



$$F \propto m_1 m_2$$

$$F \propto \frac{1}{r^2} \quad \left. \vphantom{F \propto \frac{1}{r^2}} \right\} F \propto \frac{m_1 m_2}{r^2}$$

$$F = \frac{G m_1 m_2}{r^2} \quad G = \text{Gravitational constant}$$

$$G = 6.67 \times 10^{-11} \frac{\text{Nm}^2}{\text{kg}^2}$$

\vec{r} = Position vector of ' m_2 ' w.r.t ' m_1 '.

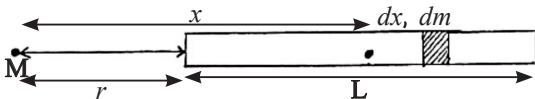
$$|\vec{F}_1| = |\vec{F}_2| = F = \frac{G m_1 m_2}{r^2}$$

$$\vec{F}_{21} = \left(\frac{G m_1 m_2}{r^2} \right) (-\hat{r})$$

$$\vec{F}_{21} = \frac{-G m_1 m_2}{r^3} \vec{r}$$

$$\vec{F}_{12} = \frac{G m_1 m_2}{r^3} \vec{r}$$

$$F \neq \frac{GMm}{\left(r + \frac{L}{2}\right)^2} \quad \because \quad L \rightarrow m$$



$$dF = \frac{GM \cdot dm}{x^2} \quad L \rightarrow \frac{M}{L} dx = dm$$

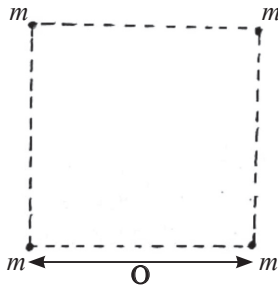
$$F = \int_r^{(r+L)} \frac{GM}{x^2} \frac{M}{L} dx = \frac{GMm}{L} \int_r^{(r+L)} \frac{dx}{x^2}$$

$$F = \frac{GMm}{L} \left[\frac{-1}{x} \right]_r^{r+L} = \frac{GMm}{L} \left[\frac{1}{r} - \frac{1}{(r+L)} \right]$$

$$F = \frac{GMm}{L} \left[\frac{r+L-r}{r(r+L)} \right] = \frac{GMm}{r(r+L)}$$

Ques.: Three masses, each equal to m are placed at three corners of a square of side a . Calculate the force of attraction on the mass placed at fourth corner.

Solns.:

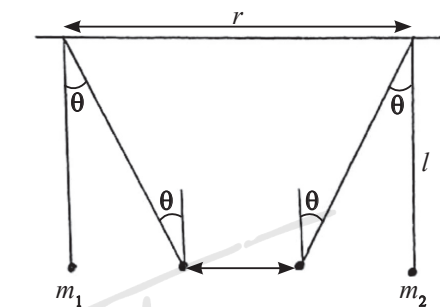


$$F = \frac{Gmm}{a^2}$$

$$F' = \frac{Gmm}{(\sqrt{2}a)^2}$$

$$F = 2F + F'$$

Ques.:



$$F = \frac{Gm^2}{(r')^2}$$

$$F = T \sin \theta \quad \dots(1)$$

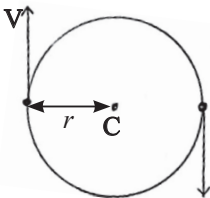
$$mg = T \cos \theta \quad \dots(2)$$

$$T^2 = F^2 + (mg)^2 \Rightarrow T = \sqrt{F^2 + (mg)^2}$$

$$\tan \theta = \frac{F}{mg} = \frac{G m_1 m_2}{(r')^2 \times m_1 \times g} = \frac{G m_2}{(r')^2 \times g}$$

Ques.: 2 particles, each of mass m goes around in a circular motion their mutual gravitational attraction. Find the value of speed with which particle is doing circular motion.

Solns.:



$$F = \frac{Gm^2}{r^2}$$

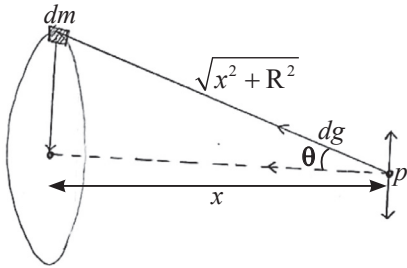
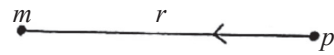
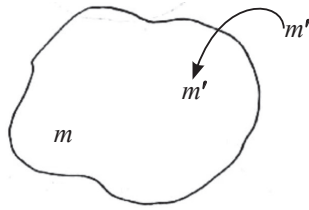
$$\frac{M \times v^2}{r} = \frac{Gm^2}{(2r)^2}$$

$$v^2 = \frac{Gm}{4r} \Rightarrow \boxed{\frac{1}{2} \sqrt{\frac{Gm}{r}} = v}$$

Gravitational Field:

- * It is region in surrounding of mass where if any other mass comes, it experiences gravitational force.

Gravitation



$$g = \frac{Gm}{r^2}$$

$$dg = \frac{Gdm}{(x^2 + R^2)}$$

$$g_p = \int dg \cos \theta$$

$$g_p = \int \frac{Gdm}{R^2 + x^2} \cdot \frac{x}{(x^2 + R^2)^{1/2}} = \frac{Gx}{(R^2 + x^2)^{3/2}} (m)$$

$$g_p = \frac{Gmx}{(R^2 + x^2)^{3/2}}$$

Sphere:

Case-1: Hollow Sphere:

1.

$x > R$ (outside)

$$g_p = \frac{Gm}{x^2}$$

2.

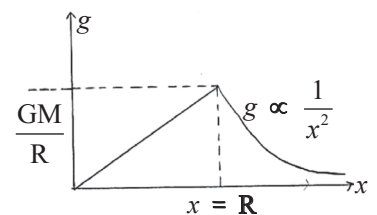
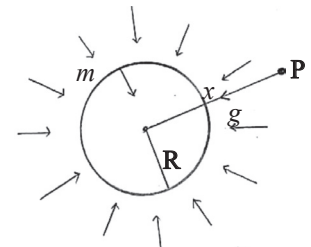
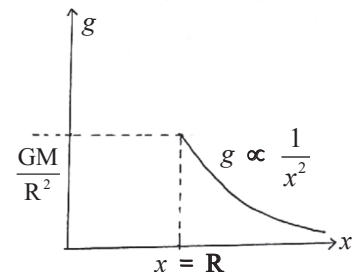
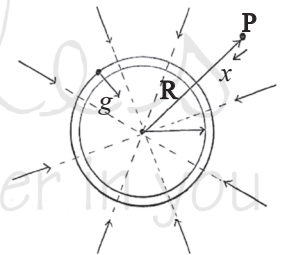
$x = R$ (surface)

$$g_s = \frac{Gm}{R^2}$$

3.

$x < R$ (inside)

$$g_{in} = 0$$



Case-2: Solid Sphere:

1.

$x > R$

$$g_p = \frac{Gm}{x^2}$$

2.

$x = R$

$$g_s = \frac{Gm}{R^2}$$

3.

$$x < R$$

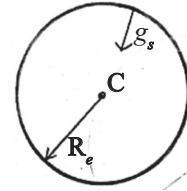
$$g_{in} = \frac{Gmx}{R^3} \Rightarrow gm \propto x$$

Earth:

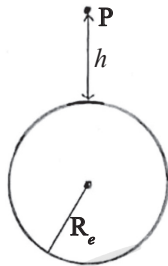
i.

$$g_s = \frac{GM_e}{R_e^2}$$

$$g_s \text{ (according to gravity)} = 9.8 \text{ m/s}^2$$



ii.



$$g_p = \frac{GM_e}{(R_e + h)^2}$$

$$g_p = \frac{GM_e}{R_e^2 \left(1 + \frac{h}{R_e}\right)^2}$$

⇒

$$g_p = \frac{g_s}{\left(1 + \frac{h}{R_e}\right)^2}$$

$$(1 + x)^n = 1 + nx \text{ if } h \ll R_e$$

$$g_p = g_s \left(1 + \frac{h}{R_e}\right)^{-2}$$

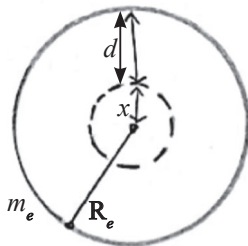
∴

$$\frac{h}{R_e} \lll 1$$

⇒

$$g_p = g_s \left(1 - \frac{2h}{R_e}\right)$$

iii.



$$g_{in} = \frac{G \cdot M_e \cdot x}{R_e^3}$$

$$x = R_e - d$$

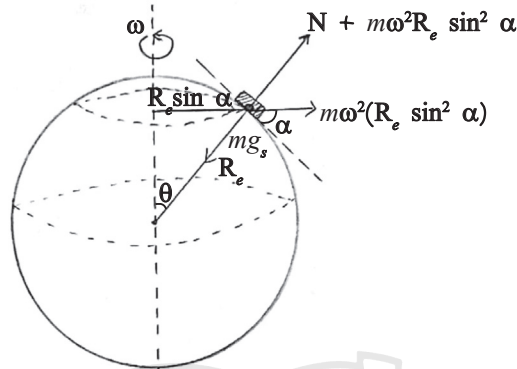
$$g_{in} = \frac{GM_e(R_e - d)}{R_e^2 \cdot (R_e)} = g_s \left(1 - \frac{d}{R_e}\right)$$

$$g_{in} = g_s \left(1 - \frac{d}{R_e}\right)$$

Effect of Rotation of Earth on the Value of g :

$$N + m\omega^2 R_e \sin^2 \alpha = Mg_s$$

$$mg_{\text{eff}} = N = mg_s - m\omega^2 R_e \sin^2 \alpha$$



$$g_{\text{eff}} = g_s - \omega^2 R_e \sin^2 \alpha$$

$$\alpha = 90^\circ$$

At equator,

\therefore

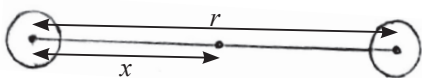
$$g_{\text{eff}} = g_s - \omega^2 \cdot R_e \quad (9.6 \text{ m/s}^2)$$

At poles

$$\alpha = 0^\circ$$

\therefore

$$g_{\text{eff}} = g_s \quad (9.8 \text{ m/s}^2)$$

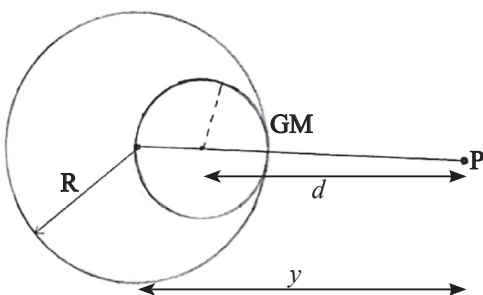


$$\frac{GM_e}{x^2} = \frac{GMm}{(r-x)^2}$$

$$x = \dots\dots\dots$$

$$(1 + x)^n = 1 + nx$$

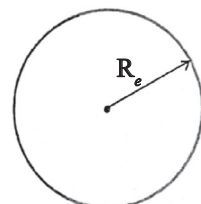
$$x \lll 1$$



$$g_{\text{big}} - g_{\text{small}}$$

$$= \frac{GM}{y^2} - \frac{GM}{8d^2}$$

$$g_s = \frac{GM_e}{R_e^2}$$



If radius of earth shrinks by 1% mass remains same.

$$g' = \frac{GM_e}{(0.99R_e)^2} = \frac{GM_e}{R_e^2(0.99^2)}$$

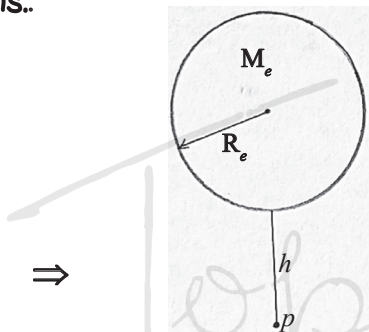
$$g' = \frac{g_s}{(1-0.01)^2} = g_s(1-0.01)^{-2}$$

$$g' = g_s(1+0.02) = g_s(1.02)$$

$$g' = g_s \left(\frac{102}{100} \right)$$

Ques.: At what height above the earth's surface value of gravitational force will be half of its value at the surface of the earth?

Solns.:



⇒

⇒

$$g_s = \frac{GM_e}{R_e^2}$$

$$\frac{g_s}{2} = g_p = \frac{g_s}{\left(1 + \frac{h}{R_e}\right)^2}$$

$$\sqrt{2} = 1 + \frac{h}{R_e}$$

$$h = (\sqrt{2} - 1)R_e$$

Ques.: With what angular velocity earth will rotate so that app. value of g at its equator becomes 0?

Solns.:

$$g_{\text{eff}} = g_s \text{ (at surface)}$$

$$g_{\text{eff}} = g_s - \omega^2 R_e \sin^2 \alpha$$

1 (\because at equator $\alpha = 90^\circ$)

$$g_s - \omega^2 R_e = 0$$

⇒

$$\omega = \sqrt{\frac{g}{R_e}}$$

Gravitational Potential Energy or Gravitational Interaction Energy:

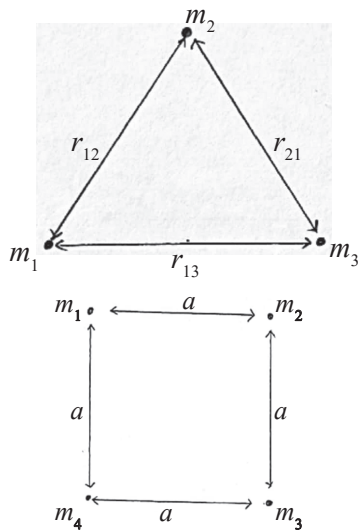
* Defined as the amount of work required to bring the particle from infinity to desired.

Case-I:

$$U = \frac{-Gm_1m_2}{r}$$

Gravitation

Cose-II:



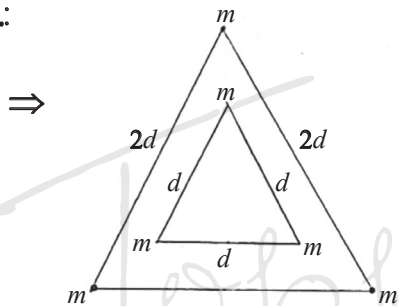
Multiple particle system:

$$U = \frac{-Gm_1m_2}{r_{12}} - \frac{Gm_2m_3}{r_{23}} - \frac{Gm_3m_1}{r_{13}}$$

$$U = \frac{-Gm_1m_4}{a} - \frac{Gm_1m_2}{\sqrt{2}a} - \frac{Gm_2m_3}{\sqrt{2}a} - \frac{Gm_4m_3}{a} - \frac{Gm_1m_3}{\sqrt{2}a} - \frac{Gm_2m_4}{\sqrt{2}a}$$

Ques.: Find W done in ↑sing the sides of triangle form d to 2d?

Solns.:



$$W = U_f - U_i$$

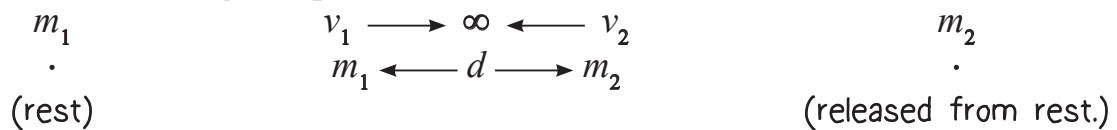
$$U_i = \frac{-Gm^2}{d} - \frac{Gm^2}{d} - \frac{Gm^2}{d} = \frac{-3Gm^2}{d}$$

$$U_f = \frac{-3Gm^2}{2d}$$

$$\text{Work done} = \frac{-3Gm^2}{2d} + \frac{3Gm^2}{d} = \frac{-3Gm^2 + 6Gm^2}{2d}$$

$$\text{Work done} = \frac{3Gm^2}{2d}$$

Ques.: Find the velocity of m_1 & m_2 when the separation between them becomes d.



Solns.:

$$U_f = \frac{-Gm_1m_2}{d}, U_i = 0, K_i = 0$$

$$E_i = 0$$

$$E_f = \frac{1}{2}m_1v_1^2 + \frac{1}{2}m_2v_2^2 - \frac{Gm_1m_2}{d} = 0 \quad \dots(1)$$

∴
⇒ ∴ Ext. force is absent, $P_i = P_f$

$$0 + 0 = m_1v_1 - m_2v_2$$

$$m_1v_1 = m_2 \cdot v_2$$

$$\Rightarrow v_1 = \frac{m_1 m_2}{m_1}$$

$$\frac{1}{2} m_1 \left(\frac{m_2^2 v_2^2}{m_1^2} \right) + \frac{1}{2} m_2 v_2^2 - \frac{G m_1 m_2}{d} = 0$$

$$\frac{1}{2} \frac{m_2 v_2^2}{m_1} + \frac{1}{2} v_2^2 = \frac{G m_1}{d}$$

$$\Rightarrow v_2^2 = \frac{2 G m_1}{d \left(\frac{m_2 + m_1}{m_1} \right)}$$

$$v_2 = \sqrt{\frac{2 G m_1^2}{d (m_2 + m_1)}} = m_1 \sqrt{\frac{2 G}{d (m_2 + m_1)}}$$

$$v_1 = m_2 \sqrt{\frac{2 G}{d (m_2 + m_1)}}$$

$$0 = \frac{1}{2} m_1 v_1^2 - \frac{G m_1 m_2}{d}$$

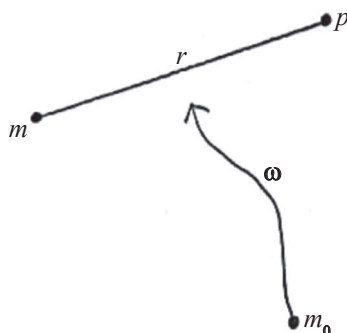
$$\Rightarrow \frac{1}{2} v_1^2 = \frac{G m_2}{d}$$

$$\Rightarrow v_1 = \sqrt{\frac{2 G m_2}{d}}$$

Gravitational Potential:

* W done in bringing a unit mass from ∞ to the given location.

Interactional Energy of Unit Mass:



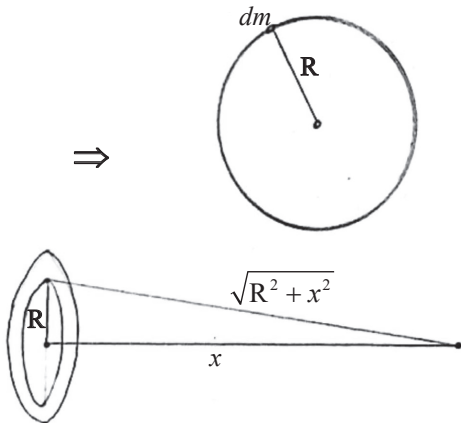
$$m_0 \rightarrow U$$

$$1 \rightarrow \frac{U}{m_0} = V_p$$

$$V_p = \frac{G m m_0}{r m_0} = \frac{-G m}{r}$$

Gravitation

Ring:



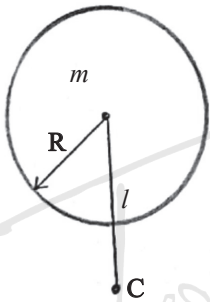
$$dV = \frac{-G \cdot dm}{R}$$

$$V = \int dV = \frac{-Gm}{R}$$

$$dV = \frac{-Gdm}{\sqrt{R^2 + x^2}}$$

$$\int dV = V = \frac{-Gm}{\sqrt{R^2 + x^2}}$$

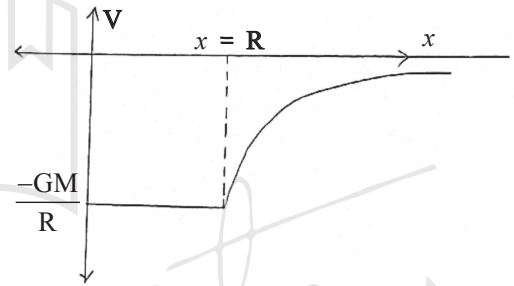
Hollow Sphere:



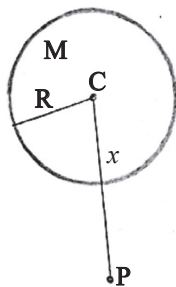
(i) $x > R, V_p = \frac{-Gm}{x}$

(ii) $x = R, V_p = \frac{-Gm}{R}$

(iii) $x = R, V_p = \frac{-Gm}{R}$



Solid Sphere:

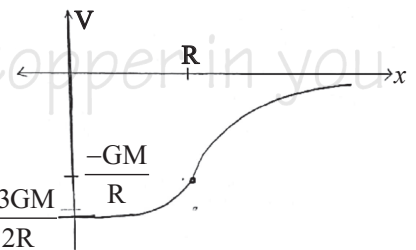


(i) $x > R, V_p = \frac{-Gm}{x}$

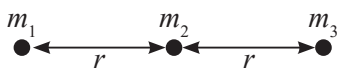
(ii) $x = R, V_p = \frac{-Gm}{R} = V_s$

(iii) $x < R, V_p = \frac{-Gm(3R^2 - x^2)}{2R^3}$

(iv) $x = 0, V_p = \frac{-3}{2} \frac{Gm}{R} = \frac{-3}{2} V_s$



Golden Key Point:



⇒

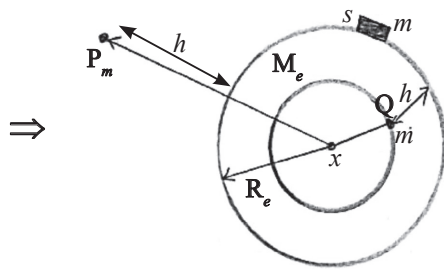
$$V = \frac{U}{m}$$

$$U = mV$$

$$U_p = m_2 V_p$$

$$U_p = m_2 \left[\frac{-Gm_1}{r} - \frac{Gm_3}{r} \right]$$

Potential Energy of a Body in Earth's Gravitational Field:



$$V = \frac{U}{m}$$

$$U = mV$$

$$U_s = mV_s = m \left(\frac{-GM}{R_e} \right) = \frac{-GMm}{R_e}$$

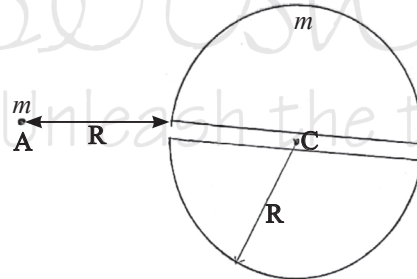
$$U_p = mV_p$$

$$\Rightarrow U_p = m \left[\frac{-GM}{R_e + h} \right]$$

$$U_Q = U_{in} = m \left[\frac{-GM}{2R^3} (3R^2 - x^2) \right]$$

$$x = R_e - h$$

Find the velocity of particle when it just crosses the centre.



$$\Rightarrow mV_A = mV_C + \frac{1}{2}mV^2$$

$$\frac{-Gm}{R} = \frac{-3Gm}{R} + \frac{V^2}{2}$$

$$V^2 = \frac{-Gm}{R} + \frac{3Gm}{R} = \frac{2Gm}{R}$$

$$\Rightarrow V = \sqrt{\frac{2Gm}{R}}$$

Gravitation

Ques.: Find out the work done in shifting from P to Q?

Solns.:

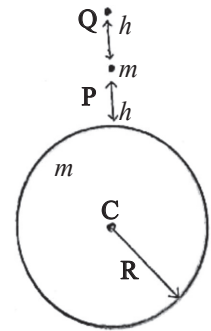
$$\Rightarrow U_f = \frac{-GMm}{R+2h}, U_i = \frac{-GMm}{R+h}$$

$$\Rightarrow W = U_f - U_i$$

$$\Rightarrow W = \frac{-GMm}{R+2h} + \frac{GMm}{R+h}$$

$$W = GMm \left(\frac{-R-h+R+2h}{(R+2h)(R+h)} \right)$$

$$= \frac{GMmh}{(R^2+3Rh+2h^2)}$$



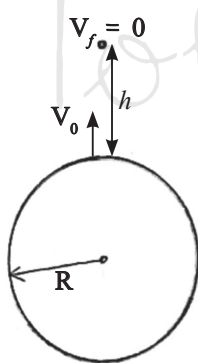
Ques.: If a particle is projected from the surface of earth with velocity V_0 , find the maximum height to which the particle will rise?

Solns.:

$$\Rightarrow \frac{1}{2} m V_0^2 - \frac{GMm}{R} = \frac{-GMm}{R+h}$$

$$\Rightarrow \frac{1}{2} V_0^2 = GM \left(\frac{-R+R+h}{R^2+Rh} \right) = \frac{GMh}{(R^2+Rh)}$$

$$\Rightarrow V_0 = \sqrt{\frac{2GMh}{R^2+Rh}}$$



Ques.: From the centre of ring, a point mass is projected such that it will escape to infinity. Find out that velocity?

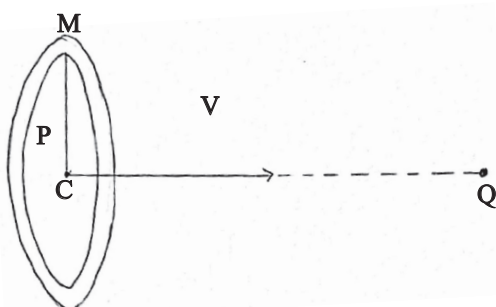
Solns.:

$$\Rightarrow \epsilon_1 = K + P$$

$$= \frac{1}{2} mV^2 + m(V_f) = 0$$

$$= \frac{1}{2} mV^2 + m \left(\frac{-Gm}{R} \right) = 0$$

$$V = \sqrt{\frac{Gm}{R}}$$



Satellite:

$r \rightarrow$ orbital radius

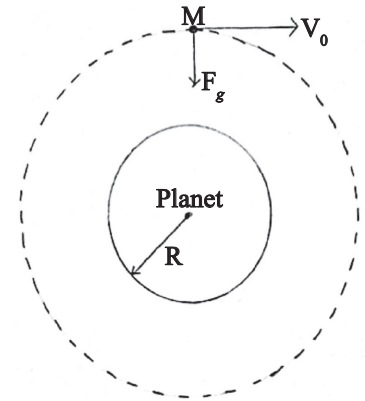
$V \rightarrow$ orbital speed

$$F_g = \frac{mV_0^2}{r}$$

\Rightarrow

$$\frac{GMm}{r^2} = \frac{-mV_0^2}{r}$$

$$V_0 = \sqrt{\frac{GM}{r}}$$



Note: It is independent of the mass of the satellite.

Orbital Period:

\Rightarrow

$$T = \frac{2\pi}{\omega} = \frac{2\pi r}{V} = \frac{2\pi \cdot r^{3/2}}{\sqrt{GM}}$$

$$\boxed{T \propto r^{3/2}} \quad (\text{Kepler laws})$$

Energy of Satellite:

KE of satellite;

$$K = \frac{1}{2}mV_0^2 = \frac{1}{2} \frac{mGM}{r}$$

$$K = \frac{GMm}{2r}$$

$$\text{PE of sat.} = P = \frac{-GMm}{r}$$

$$\text{Total energy} = E_T = \frac{-GMm}{2r}$$

$$\boxed{|E_T| = |KE| = \frac{1}{2}|PE|}$$

Gravitation

Ques.: A satellite is revolving around earth in orbital radius in $4R_e$. Find its orbital speed & time period?

Solns.: \Rightarrow

$$V_0 = \sqrt{\frac{GM}{r}} = \sqrt{\frac{gr^2}{4R_e}}$$

$$= \sqrt{\frac{gR_e \times R_e}{4R_e}} = \sqrt{\frac{gR_e}{4}}$$

$$V_0 = \frac{1}{2}\sqrt{gR_e}$$

Time period: $\frac{2\pi(4 \times R_e)^{3/2}}{\sqrt{gR_e^2}} = \frac{2\pi(4R_e)^{3/2}}{\sqrt{gR_e^2}}$

$$= 16\pi \sqrt{\frac{R_e}{g}}$$

Ques.: Two satellites A & B of same mass are orbiting around earth at altitudes R & $3R$. Calculate the ratio of KE of A & B?

Solns.: \Rightarrow

$$KE_A = \frac{GMm}{R + R_e}$$

$$KE_B = \frac{GMm}{3R + R_e}$$

$$\frac{KE_A}{KE_B} = \frac{3R + R_e}{R + R_e} = \frac{4R}{2R} = \frac{2}{1}$$

\Rightarrow $2 : 1$

Ques.: A satellite of mass 2×10^3 kg is to be shifted from an orbit of radius $2R_e$ to $3R_e$. Find out the minimum energy required to shift?

Solns.: \Rightarrow

$$E = \frac{-GMm}{2 \times 2R_e} + \frac{GMm}{6R_e}$$

$$= + GMm \left[\frac{-3 + 2}{12R_e} \right]$$

$$E = \frac{-GMm}{12R_e}$$

Bounded Motion and Escape Velocity:

- * Total energy of mass 'm' at the surface = K + P

$$E_T = \frac{1}{2}mV^2 - \frac{GMm}{R} < 0$$

If somehow we implant KE such that its total energy = 0

$$\frac{1}{2}mV_e^2 - \frac{GMm}{R} = 0$$

⇒

$$V_{\text{escape}} = \sqrt{\frac{2GM}{R}}$$

Planet = Earth

$$V_{\text{escape}} = \sqrt{\frac{2GM}{R_e}} = \sqrt{2g_s \cdot R_e} = 11.2 \text{ Km/sec.}$$

$$V_0 = -\sqrt{\frac{GM}{r}}$$

$$TE = \frac{-GMm}{2r}$$

If some how speed of satellite is increased from $V_0 \rightarrow V_{\text{escape}}$

$$\frac{1}{2}mV_e^2 - \frac{GMm}{r} = 0$$

$$V_{\text{es}} = \sqrt{\frac{2GM}{r}}$$

$$V_{\text{es}} = \sqrt{2}V_0$$

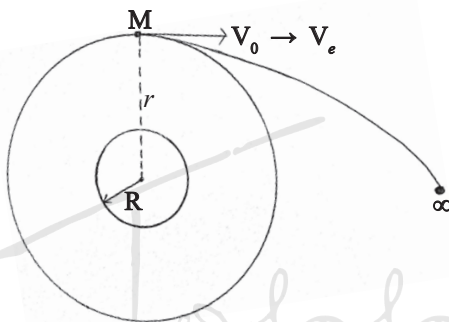
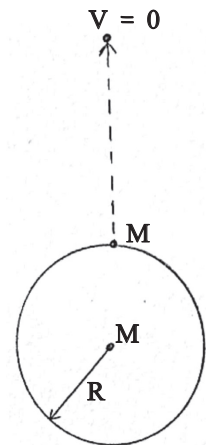
Increase in speed of satellite = ΔV

$$= \sqrt{2}V_0 - V_0 = V_0(\sqrt{2} - 1)$$

$$= V_0 \times 0.414$$

$$\Delta V = 41.4 \% V_0$$

- * If orbital velocity of a satellite is increased by 41.4%, then it escapes from the gravitational field of earth.



Gravitation

Ques.: An artificial satellite is moving around earth in a circular orbit such that its speed is equal to half of the escape velocity from the earth. Find the height of the satellite.

Solns.: \Rightarrow

$$V_0 = \frac{1}{2} V_{\text{escape}}$$

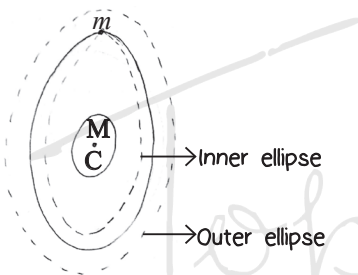
$$\sqrt{\frac{GM}{R+h}} = \frac{1}{2} \sqrt{\frac{GM}{R}}$$

$$\frac{GM}{R+h} = \frac{1}{4} \left(\frac{GM}{R} \right)$$

$$2R = R + h$$

$R = h$

Motion of Satellite in an Elliptical Path:



(if $V_0 < V_s < V_{\text{esc}}$)

$$\frac{mV_0^2}{r} > F_g$$

(if $V_s < V_0$)

$F_g > \frac{mV_0^2}{r}$

Angular Momentum in Case of Satellite Motion:

The only force acting is gravitational force.

$$\vec{\tau} F_g = 0$$

\Rightarrow

$$L_i = L_f$$

$$L = m(\vec{r} \times \vec{v}) = mvr \sin \theta$$

$$L = mvr \sin \theta = mV_{\text{max}} r_{\text{min}}$$

$$= mV_{\text{min}} r_{\text{max}} = \text{constant}$$

$$G = \frac{1}{2} mV^2 - \frac{GMm}{r} = \frac{1}{2} mV_{\text{min}}^2 - \frac{GMm}{r_{\text{max}}}$$

$$= \frac{1}{2} mV_{\text{max}}^2 - \frac{GMm}{r_{\text{min}}}$$

